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| Re : | Consolidation of contributions submitted in response to call IEEE 802.16m-08/042, "Call for Contributions on Project 802.16 m Draft Amendment Content" providing text for the topic of "Downlink Physical Structure" |
| Abstract | The contribution provides PHY structure text for the IEEE 802.16 m amendment. Highlighted text is not agreed and will not be included in the draft. |
| Purpose | To be incorporated into the initial IEEE 802.16 amendment as directed in Session 58 |
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# PHY Structure text for the IEEE 802.16m Amendment 

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## 1. Introduction

This contribution is the output of the TGm drafting group that has worked to consolidate contributions that have provided detailed Stage 3 text on DL PHY Structure and UL PHY Structure.

## 2. Outline

The following is the high level outline of the DL PHY structure:

15.3.5. Downlink physical structure<br>15.3.5.1 Physical and Logical Resource Unit<br>15.3.5.1.1 Distributed Resource Unit<br>15.3.5.1.2 Contiguous Resource Unit<br>15.3.5.2 Multi-cell Resource Mapping<br>15.3.5.2.1. Subband partitioning<br>15.3.5.2.2. Miniband permutation<br>15.3.5.2.3. Frequency partitioning<br>15.3.5.3 Cell-Specific Resource Mapping<br>15.3.5.3.1. CRU/DRU allocation<br>15.3.5.3.2. Secondary permutation<br>15.3.5.3.3. Subcarrier permutation

## 3. Contribution List

4 The following contributions were identified as containing detailed DL PHY Structure text:

| Section 5 | Section 5 |
| :--- | :--- |
| Source Document Authors | Source Document Reference |
| Mark Cudak, et. al. | IEEE C802.16m-08/1441 |
| J. K. Fwu, et. al. | IEEE C802.16m-08/1443r2 |
| Guan Yanfeng, et. al., | IEEE C802.16m-08/1448r1 |
| Lai-Huei Wang, et. al. | IEEE C802.16m-08/1449r1 |
| Xin Qi, et. al. | IEEE C802.16m-08/1450r1 |
| Taeyoung Kim, et. al. | IEEE C802.16m-08/1464r3 |
| HanGyu Cho, et. al | IEEE C80216m-07/1466r1 |

## Text proposal for inclusion in the 802.16m amendment

$\qquad$

Insert a new section 15:

## 15. Advanced Air Interface

### 15.3. Physical layer

### 15.3.5. Downlink physical structure

Each downlink subframe is divided into 4 (TBD) or fewer frequency partitions; each partition consists of a set of physical resource units across the total number of OFDMA symbols available in the subframe. Each frequency partition can include contiguous (localized) and/or non-contiguous (distributed) physical resource units. Each frequency partition can be used for different purposes such as fractional frequency reuse (FFR) or multicast and broadcast services (MBS). Figure 15.3.5.1 illustrates the downlink physical structure in the example of two frequency partitions with frequency partition 2 including both contiguous and distributed resource allocations.


Figure 1 - Example of downlink physical structure

### 15.3.5.1. Physical and logical resource unit

A physical resource unit (PRU) is the basic physical unit for resource allocation that comprises Psc consecutive subcarriers by $N s y m$ consecutive OFDMA symbols. $P s c$ is 18 subcarriers and $N_{s y m}$ is 6 OFDMA symbols for type-1 subframes, and Nsym is 7 OFDM symbols for type-2 sub frames. A logical resource unit (LRU) is the basic logical unit for distributed and localized resource allocations. A LRU is $P s c \bullet N s y m$ subcarriers for type-1 subframes and type-2 subframes. The LRU includes the pilots in 15.3.5.3 that are used in a PRU. The effective number of subcarriers in an LRU depends on the number of allocated pilots.

### 15.3.5.1.1. Distributed resource unit

The distributed resource unit (DRU) contains a group of subcarriers which are spread across the distributed resource allocations within a frequency partition. The size of the DRU equals the size of PRU, i.e., Psc subcarriers by Nsym OFDMA symbols. The minimum unit for forming the DRU is equal to a pair of subcarriers, called tone-pair, as defined in 15.3.5.2.3.1.

### 15.3.5.1.2. Contiguous resource unit

The localized resource unit, also known as contiguous resource unit (CRU), contains a group of subcarriers which are contiguous across the localized resource allocations. The size of the CRU equals the size of the PRU, i.e., Psc subcarriers by Nsym OFDMA symbols.

### 15.3.5.2. Multi-cell resource mapping

### 15.3.5.2.1. Subband partitioning

The physical PRUs are first subdivided into subbands and minibands where a subband comprises $N_{1}$ adjacent PRUs and a miniband comprises $N_{2}$ adjacent PRUs, where $N_{1}=4$ [or 8 for the 2048 FFT] \& $N_{2}=1$ [or 2 for the 2048 FFT]. Subbands are suitable for frequency selective allocations as they provide a contiguous allocation of PRUs in frequency. Minibands are suitable for frequency diverse allocation and are permuted in frequency.

The number of subbands reserved is denoted by $K_{S B}$. The number of PRUs allocated to subbands is denoted by $L_{\mathrm{SB}}$, where $L_{\mathrm{SB}}=N_{1} * K_{\mathrm{SB}}$. A 5-bit (TBD) field called Subband Allocation Count (SAC) field determines the value of $K_{\mathrm{SB}}$. The SAC is transmitted in the BCH. The remainder of the PRUs are allocated to minibands. The number of minibands in an allocation is denoted by $K_{\mathrm{MB}}$. The number of PRUs allocated to minibands is denoted by $L_{\mathrm{MB}}$, where $L_{\mathrm{MB}}=N_{2} * K_{\mathrm{MB}}$. The total number of PRUs is denoted as $\mathrm{N}_{\mathrm{PRU}}$ where $\mathrm{N}_{\mathrm{PRU}}=\mathrm{L}_{\mathrm{SB}}+$ $\mathrm{L}_{\mathrm{MB}}$. [The mapping of the BCH is FFS and may be incorporated in the partitioning process.]

PRUs are partitioned and reordered into two groups subband PRUs and miniband PRUs, denoted PRU ${ }_{S B}$ and $\mathrm{PRU}_{\mathrm{MB}}$, respectively. The set of $\mathrm{PRU}_{\mathrm{SB}}$ is numbered from 0 to $\left(L_{S B}-1\right)$. The set of $\mathrm{PRU}_{\mathrm{MB}}$ are numbered from 0 to $\left(L_{M B}-1\right)$. Equation 1 defines the mapping of PRUs to $P_{R B} S$. Equation 2 defines the mapping of PRUs to $\mathrm{PRU}_{\mathrm{MB}} \mathrm{S}$. Figure 2 illustrates the PRU to $P R U_{S B}$ and $P R U_{M B}$ mapping for a 5 MHz bandwidth with SAC equal to 3 .

$$
P R U_{S B}[j]=P R U[i], \quad j=0,1, \ldots, L_{S B}-1, \ldots \ldots \ldots \ldots \ldots . . \text { Eqn. (1) }
$$

## [Editor's note: following option is proposed in 1441]



## In Option 1:

Let $N_{\text {sut }}$ be the maximum number of subbands that can be formed and $N_{\text {sub }}=N_{\text {PRU }} / N_{1}$.

$$
i=\operatorname{PermUniform}\left(N_{\text {sub }}, K_{S B} ;\left\lfloor j / N_{1}\right\rfloor\right) \quad N_{1}+\{j\} \bmod N_{1},
$$

where PermUniform $(L, K ; \cdot)$ is a permutation function whose $K$ elements are chosen evenly among all $L$ elements:

and $\operatorname{GCD}(\mathrm{x}, \mathrm{y})$ is the greatest common divisor of x and y .

## In Option 2:

$$
i=\left\{\begin{array}{cc}
\left\lfloor j / N_{1}\right\rfloor N_{2}\left\lceil N_{P R U} /\left(N_{2} * K_{S B}\right)\right\rceil+\{j\} \bmod \left(N_{1}\right) & \text { for } j<\left(\left\{N_{P R U} / N_{2}\right\} \mathrm{m}\right. \\
\left\lfloor j / N_{1}\right\rfloor N_{2}\left\lfloor N_{P R U} /\left(N_{2} * K_{S B}\right)\right\rfloor+\{j\} \bmod N_{1}+\left(\left\{N_{P R U} / N_{2}\right\} \bmod \left(K_{S B}\right)\right) N_{2} & \text { for } j \geq\left(\left\{N_{P R U} / N_{2}\right\} \mathrm{m}\right.
\end{array}\right.
$$

[Editor's note: following option is proposed in 1464r3...]

| where |
| :--- |
| w |
| $=N_{1} \cdot N_{\text {dist }} \cdot\left(\left\lfloor\frac{j}{N_{1}}\right\rfloor \bmod \frac{N_{\text {sub }}}{N_{\text {dist }}}\right)+N_{1} \cdot\left\lfloor\frac{N_{\text {dist }}}{N_{\text {sub }}} \cdot \frac{j}{N_{1}}\right\rfloor+\left(j \bmod N_{1}\right)$ | (Eq. 2)

where

[Editor's note: following option is proposed in 1466rl]
where

where.
$G C D(x, y)$ is the greatest common divisor of $x$ and $y$.


$$
P R U_{M B}[k]=P R U[i], \quad k=0,1, \ldots, L_{M B}-1,
$$

Eqn. (2) [Editor's note: following option is proposed in 1441]


## where

In Option 1:
$i=\operatorname{PermUniform}\left(N_{\text {sub }}, K_{S B} ; K_{S B}+\left\lfloor k / N_{1}\right\rfloor\right) N_{1}+\{k\} \bmod N_{1}$

## In Option 2:

After $P R U_{S B}$ are selected, the remaining PRUS are renumbered and assigned as PRU $U_{M B}$ without reordering.
EEditor's note: following option is proposed in 1448r1...]

[Editor's note: following option is proposed in 1464r3...]
where the relationship equation between $i$ and $k$ is same as the equation (1) except for $j=k+L_{S B}$.
[Editor's note: following option is proposed in 1466rl]
where



Figure 2 PRU to $\mathrm{PRU}_{\mathrm{SB}}$ and $\mathrm{PRU} \mathrm{U}_{\text {MB }}$ mapping for $\mathrm{BW}=5 \mathrm{MHz}, \mathrm{SAC}=3$

### 15.3.5.2.2. Miniband permutation

The miniband permutation maps the $\mathrm{PRU}_{\mathrm{MB}} \mathrm{S}$ to Permuted $\mathrm{PRU}_{\mathrm{MB}} \mathrm{S}\left(\mathrm{PPRU}_{\mathrm{MB}} \mathrm{S}\right)$ to insure frequency diverse PRUs are allocated to each frequency partition. Equation (3) provides a mapping from $\mathrm{PRU}_{\mathrm{MB}}$ to $\mathrm{PPRU}_{\mathrm{MB}} S$

$$
P P R U_{M B}[j]=P R U_{M B}[i], \quad j=0,1, \ldots, L_{M B}-1 \quad \text { Eqn } 3
$$

[Editor's note: following option is proposed in 1441]
$\square$
[Editor's note: following option is proposed in 1443r2...

## where

$i=\operatorname{PermSeq}\left(\left\lfloor j / N_{2}\right\rfloor\right) \quad N_{2}+\{j\} \bmod N_{2}$
and $\operatorname{PermSeq}(\mathrm{k})$ is the k -th elelment of the S-Random permutation sequence of length $L_{\mathrm{MB}}$ from Table 15.3.5.1. Sequences of different length are tabulated in Table 15.3.5.1


where

[Editor's note: following option is proposed in 1449r1...]
where


$$
\begin{aligned}
& i=(q(j) \bmod D) \cdot F P C T+\left\lfloor\frac{q(j)}{D}\right\rfloor, j=0,1, \ldots, K_{M B}-1 \\
& q(j)=j+\left\lfloor\frac{r(j)}{D-1}\right\rfloor, \\
& r(j)=\max \left(j-\left(L_{M B} \bmod (F P C T)\right) \cdot D, 0\right), \\
& D=\left\lfloor\frac{L_{M B}}{F P C T}+1\right\rfloor
\end{aligned}
$$

Where FPCT denotes the number of frequency partition.
[Editor's note: following option is proposed in 1466r1...
$i=(q(j) \bmod D) \cdot(F 1$

Deleted: | $q(j)=j+\left\lfloor\frac{r(j)}{D-}\right.$ |
| ---: |
| $r(j)=\max (j-1$ |
| $D=\left\lfloor\frac{L_{M B}}{F F R C+1}\right.$ |
| Deleted: $i=\frac{N_{1}}{N_{2}} \times\left\lfloor\frac{j}{N_{2}}\right\rfloor \bmod K_{M}$ |

$i=N_{2} \cdot\left\{F P C T \cdot\left\lfloor\frac{j}{N_{2}}\right\rfloor+\left\lfloor\left\lfloor\frac{j}{N_{2}}\right\rfloor \cdot \frac{G C D\left(K_{M B}, F P C T\right)}{K_{M B}}\right\rfloor\right\} \bmod K_{M B}+j \bmod N_{2}$.
where $F P C T$ denotes the number of frequency partitions.

Figure 3 depicts the mapping from PRUs to PRUSB and PPRUMB.
Deleted: Figure 4


Figure 3 Mapping from PRUs to $\mathrm{PRU}_{\text {SB }}$ and $\mathrm{PPRU}_{\text {MB }}$ for $\mathrm{BW}=5 \mathrm{MHz}, \mathrm{SAC}=3$

### 15.3.5.2.3. Frequency partitioning

The $\mathrm{PRU}_{\text {SB }}$ and $\mathrm{PPRU}_{\text {MB }}$ are allocated to one or more frequency partitions. By default, only one partition is present. The maximum number of frequency partitions is 4 (TBD). The frequency partition configuration is transmitted in the BCH in a 12-bit called the Frequency Partition Configuration (FPC).

The FPC consists of a Frequency Partition Count (FPCT), Frequency Partition Size (FPS) and Frequency Partition Subband Count (FPSC). The first two bits carry the FPCT that defines the number of frequency partitions ( 1 to 4 ). The following 6 bits carry the FPS that defines the number of PRUs allocated to FPi, i>0 in the number of minibands (N2). The remaining 4 bits carry FPSC that define the number of subbands allocated to FPi , $\mathrm{i}>0$.

The number of subbands in i -th frequency partition are denoted by $\mathrm{K}_{\mathrm{SB}, \mathrm{FP} i}$. The number of minibands is denoted by K $_{\text {MB,FPi, }}$, which are determined by FPS and FPSC fields. The number of subband PRUs in each frequency partition is denoted by $\mathrm{L}_{\mathrm{SB}, \mathrm{FP},}$, which is given by $\mathrm{L}_{\mathrm{SB}, \mathrm{FPI}}=\mathrm{N}_{1}{ }^{*} \mathrm{~K}_{\mathrm{SB}, \mathrm{FP} \mathrm{i}}$. The number of miniband PRUs in each frequency partition is denoted by $L_{M B, F P i}$, which is given by $L_{M B, F P i}=N_{2}$ * $\mathrm{K}_{\mathrm{MB}, \mathrm{FP}}$ -
$\mathrm{K}_{\mathrm{SB}, \mathrm{FPi}}=\left\{\begin{array}{cc}S A C-(F P C T-1) \cdot F P S C & i=0 \\ F P S C & i>0\end{array}\right.$
$\mathrm{K}_{\mathrm{MB}, \mathrm{FPi}}=\left\{\begin{array}{cc}K_{M B}-(F P C T-1) \cdot\left(F P S-\frac{F P S C \cdot N 1}{N 2}\right) & i=0 \\ F P S-\frac{F P S C \cdot N 1}{N 2} & i>0\end{array}\right.$
The mapping of subband PRUs and miniband PRUs to the frequency partition $i$ is given by the following equation:
$P R U_{F P i}(j)= \begin{cases}P R U_{S B}\left(k_{1}\right) & \text { for } 0 \leq j<L_{S B, F P i} \\ P P R U_{M B}\left(k_{2}\right) & \text { for } L_{S B, F P i} \leq j<\left(L_{S B, F P i}+L_{M B, F P i}\right) \quad \text { (Eq 6) }\end{cases}$
where

$$
k_{1}=\sum_{m=0}^{i-1} L_{S B, F P m}+j
$$

and

$$
k_{2}=\sum_{m=0}^{i-1} L_{M B, F P m}+j-L_{S B, F P i}
$$

Figure 4 depicts the frequency partitioning $\mathrm{BW}=5 \mathrm{MHz}, \mathrm{SAC}=3, \mathrm{FPCT}=2, \mathrm{FPS}=12$ and $\mathrm{FPSC}=1$.


### 15.3.5.3. Cell-specific resource mapping

$\mathrm{PRU}_{\text {FPis }}$ will be mapped to LRUs. All further PRU and subcarrier permutation will be constrained to the PRUs

### 15.3.5.3.1. CRU/DRU allocation

The partition between CRUs and DRUs is done on a sector specific basis. DRU allocation is signaled in two step process.

There are four possible pre-configured allocations signaled in two bits:

| $00--$ | All $\mathrm{PRU}_{\mathrm{FPi}} \mathrm{s}$ are allocated to DRUs |
| :--- | :--- |
| $01--$ | All $\mathrm{PRU}_{\mathrm{FPi}} \mathrm{S}$ are allocated to CRUs |
| $10--$ | All subband PRUs are allocated to CRUs and all miniband PRUs are allocated to DRUs |
| $11--$ | The mapping is signaled explicitly |

When explicit mapping is indicated, additional 4-bit (TBD) CRU allocation size (CAS) field is sent in the BCH for each allocated frequency partition. CASi indicated the number of allocated CRUs for partition FPi in a unit of subband size.

The number of CRUs in each frequency partition is denoted by $\mathrm{L}_{\mathrm{CRU}, \mathrm{FPi}}$, where

$$
L_{C R U, F P_{i}}=C A S_{i}{ }^{*} N 1 \text { for } 0 \leq i<F P C T
$$

The number of DRUs in each frequency partition is denoted by $L_{D R U, F P i}$ where

$$
L_{D R U, F P i}=F P S_{i}{ }^{*} N 2-C A S_{i}{ }^{*} N 1 \text { for } 0 \leq i<F P C T
$$

The mapping of $P R U_{F P i}$ to
$C R U_{F P i}[j]=P R U_{F P i}[j]$, for $\quad 0 \leq i<F P C T, \quad$ and $\quad 0 \leq j<L_{C R U, F P i}$
$D R U_{F P i}[j]=P R U_{F P i}\left[j+L_{C R U, F P i}\right]$, for $\quad 0 \leq i<F P C T, \quad$ and $\quad 0 \leq j<L_{D R U, F P i}$

### 15.3.5.3.2. Secondary permutation

The miniband CRUs may be permuted on a sector specific basis by a secondary permutation. Permutation of the secondary permutation will be signaled by a 1 -bit secondary permutation field in the BCH .

The secondary permutation will be governed by the following equation:
TBD (eq X)

### 15.3.5.3.3. Subcarrier permutation

The subcarrier permutation defined for the DL distributed resource allocations within a frequency partition spreads the subcarriers of the DRU across the whole distributed resource allocations. The granularity of the subcarrier permutation is equal to a pair of tones.

After mapping all pilots, the remainders of the used subcarriers are used to define the distributed LRU. To allocate the LRUs, the remaining subcarriers are paired into contiguous tone-pairs. Each LRU consists of a group of tone-pairs.

Let $L_{\text {pair,l }}$ denote the number of tone-pairs in $l$-th OFDMA symbol within a PRU, i.e., $L_{\text {pair } l}=\left(P_{s c}-n_{l}\right) / 2$, where $n_{l}$ denotes the number of pilot tones in the $l$-th OFDMA symbol within a PRU. A permutation sequence PermSeq( ) is defined by [a lookup table][a sequence generation algorithm] to perform the DL subcarrier permutation as follows:

For each $l$-th OFDMA symbol in the subframe,

1. Allocate the $n_{l}$ pilots within each PRU as described in section (TBD)
2. Renumber the remaining $L_{D R U, F P, i} *\left(P s c-n_{l}\right)$ data subcarriers in order, from 0 to $L_{D R U, F P i}\left(P s c-n_{l}\right)-1$.

Group these contiguous and logically renumbered subcarriers into $L_{D R U, F P i} * L_{\text {pair, }}$ pairs and renumber them from 0 to $L_{D R U, F P, i} * L_{p a i r, l}-1$. The renumbered tone pairs in the $l$-th OFDMA symbol are denoted by $R T P_{F P, i, l}$.
3. Apply the subcarrier permutation formula (eqn. subcarrier_perm) to form the permuted tone-pairs 0 to $L_{D R U, F P, i} * L_{\text {pair },-1}-1$.
4. Map logically contiguous tone-pairs $\left[i * L_{\text {pair }, l}, \quad(i+1)^{*} L_{\text {pair, }}-1\right]$ into the $i$-th distributed LRUs, $i=0,1, \ldots$, $L_{D R U, F P i}-1$.

For the $s$-th distributed LRU of the $t$-th subframe, the subcarrier permutation formula is given by

$$
\operatorname{pair}(s, m, l, t)=L_{D R U, F P, i} * f(m, s)+g(\operatorname{PermSeq}(), s, m, l, t), l=0,1, \ldots, N_{s y m} \quad \text { Eqn(subcarrier_perm) }
$$

where $\operatorname{pair}(s, m, l, t)$ is the tone-pair index of the $m$-th tone-pair $\left(\left(0<=m<L_{\text {pair }, l}\right)\right)$ in the $l$-th OFDMA symbol $\left(0<=l<N_{s y m}\right)$ in the $s$-th distributed LRU of the $t$-th subframe; $t$ is the subframe index with respect to the frame, $s$ is the distributed LRU index ( $0<=\mathrm{s}<L_{D R U, F P, i}$ ), $m$ is the tone-pair index within the $l$-th OFDMA symbol. $\operatorname{PermSeq}()$ is the permutation sequence generated by a function or by a lookup table; $g(\operatorname{PermSeq}(), s, m, l, t)$ is a function (TBD) with value from the set $\left[0, L_{D R U, F P, i}-1\right] ; f(m, s)$ is a function (TBD) with value from the set [0, $\left.L_{\text {pair }, l}-1\right]$

The following is proposed by proposed in $1443 r 2$
$f(m, s)=\{m+13 s\} \bmod L_{\text {pair }, l}$
$g($ PermSeq, $s, m, l, t)=\left\{\left\{\operatorname{PermSeq}\left(\{f(m, s)+s+t+l\} \bmod L_{D R U, F P i}\right)\right\}+D L_{-}\right.$PermBase $\} \bmod L_{D R U, F P i}$

```
where PermSeq is the sequence of length }\mp@subsup{L}{DRU, FPi specified in Table 15.3.5.1. and DL_PermBase is an integer ranging from 0 to }{\mathrm{ fo}
(TBD), which is set to preamble IDCell or specified by the SBCH.
```

Table 15.3.5.1 Permutation sequences ( PermSeq ) of different lengths

| Size (N) | Permutation Sequence (PermSeq) |
| :---: | :---: |
| 4 | 3142 |
| 5 | $1 \begin{array}{lllll}1 & 4 & 2 & 5\end{array}$ |
| 6 | $1 \begin{array}{llllll}1 & 3 & 5 & 2 & 4\end{array}$ |
| 7 | $\begin{array}{lllllll}1 & 3 & 5 & 2 & 7 & 4\end{array}$ |
| 8 | 1 6 3 7 2 5 8 4 |
| 9 | $\begin{array}{llllllllll}7 & 4 & 1 & 8 & 5 & 2 & 9 & 6 & 3\end{array}$ |
| 10 | 1 4 7 10 3 6 9 2 5 8 |
| 11 | $\begin{array}{lllllllllll}1 & 9 & 6 & 3 & 11 & 8 & 5 & 2 & 10 & 7 & 4\end{array}$ |
| 12 | $\begin{array}{llllllllllll}1 & 7 & 4 & 11 & 8 & 5 & 2 & 12 & 9 & 3 & 6 & 10\end{array}$ |
| 13 | $\begin{array}{lllllllllllll}1 & 11 & 8 & 3 & 13 & 6 & 10 & 2 & 5 & 9 & 12 & 4 & 7\end{array}$ |
| 14 | $\begin{array}{llllllllllllll}1 & 13 & 7 & 4 & 14 & 8 & 11 & 3 & 6 & 10 & 2 & 5 & 12 & 9\end{array}$ |
| 15 | $\begin{array}{lllllllllllllll}1 & 7 & 4 & 12 & 8 & 15 & 3 & 11 & 6 & 14 & 9 & 5 & 2 & 10 & 13\end{array}$ |
| 16 | $\begin{array}{llllllllllllllll}13 & 9 & 5 & 1 & 14 & 10 & 6 & 2 & 15 & 11 & 7 & 3 & 16 & 12 & 8 & 4\end{array}$ |
| 17 | $\begin{array}{lllllllllllllllll}5 & 1 & 9 & 13 & 17 & 4 & 8 & 12 & 16 & 3 & 7 & 11 & 15 & 2 & 6 & 10 & 14\end{array}$ |
| 18 | 1 18 14 10 6 2 15 11 7 3 16 12 8 4 17 13 9 5 |
| 19 | 1 16 12 8 4 17 13 9 5 18 14 10 2 6 19 11 15 7 <br> 3                  |
| 20 | 1 7 12 16 20 5 10 14 18 3 9 13 17 2 6 11 19 15 <br> 4 8                 |
| 21 | $\begin{array}{\|cccccccccccccccccc\|} \hline 1 & 7 & 11 & 15 & 19 & 4 & 8 & 12 & 16 & 20 & 5 & 9 & 13 & 17 & 2 & 6 & 21 & 10 \\ 14 & 3 & 18 & & & & & & & & & & & & & & & \\ \hline \end{array}$ |
| 22 | $\begin{array}{\|llllllllllllllllll} 1 & 6 & 15 & 19 & 11 & 7 & 3 & 16 & 12 & 8 & 20 & 2 & 14 & 10 & 21 & 5 & 17 & 9 \\ 13 & 22 & 18 & 4 & & & & & & & & & & & & & & \\ \hline \end{array}$ |
| 23 | $\begin{array}{\|cccccccccccccccccc} 1 & 10 & 5 & 21 & 17 & 9 & 13 & 4 & 23 & 19 & 11 & 15 & 7 & 2 & 20 & 16 & 12 & 6 \\ 22 & 18 & 14 & 3 & 8 & & & & & & & & & & & & & \\ \hline \end{array}$ |

IEEE C $802.16 \mathrm{~m}-08 / 1508 \underline{\mathrm{r} 1}$

| 24 | $\begin{array}{llllllllllllllllll} 1 & 6 & 17 & 12 & 21 & 8 & 3 & 15 & 19 & 7 & 11 & 23 & 2 & 16 & 10 & 20 & 24 & 5 \\ 13 & 18 & 22 & 9 & 14 & 4 & & & & & & & & & & & & \\ \hline \end{array}$ |
| :---: | :---: |
| 25 | $\begin{array}{rrrrrrrrrrrrrrrrr} 21 & 16 & 11 & 6 & 1 & 22 & 17 & 12 & 7 & 2 & 23 & 18 & 13 & 8 & 3 & 24 & 19 \\ 14 & 9 & 4 & 25 & 20 & 15 & 10 & 5 & & & & & & & & & \\ \hline \end{array}$ |
| 26 | $\begin{array}{llllllllllllllllll} 6 & 1 & 11 & 16 & 21 & 26 & 5 & 10 & 15 & 20 & 25 & 4 & 9 & 14 & 19 & 24 & 3 & 8 \\ 13 & 18 & 23 & 2 & 7 & 12 & 17 & 22 & & & & & & & & & & \\ \hline \end{array}$ |
| 27 | $\begin{array}{rrrrrrrrrrrrrrrrrr} 6 & 1 & 11 & 16 & 21 & 26 & 5 & 10 & 15 & 20 & 25 & 2 & 7 & 12 & 17 & 22 & 27 & 4 \\ 9 & 14 & 19 & 24 & 3 & 8 & 13 & 18 & 23 & & & & & & & & & \\ \hline \end{array}$ |
| 28 | $\begin{array}{rrrrrrrrrrrrrrrrrr} 6 & 11 & 1 & 16 & 21 & 26 & 8 & 3 & 13 & 18 & 23 & 28 & 7 & 2 & 12 & 17 & 22 & 27 \\ 5 & 10 & 15 & 20 & 25 & 4 & 9 & 14 & 19 & 24 & & & & & & & & \\ \hline \end{array}$ |
| 29 | $\begin{array}{llllllllllllllllll} 1 & 6 & 11 & 16 & 21 & 26 & 5 & 10 & 15 & 20 & 25 & 4 & 9 & 14 & 19 & 24 & 29 & 2 \\ 12 & 7 & 18 & 23 & 28 & 13 & 3 & 8 & 22 & 27 & 17 & & & & & & & \\ \hline \end{array}$ |
| 30 | $\begin{array}{llllllllllllllllll} 1 & 6 & 19 & 24 & 29 & 12 & 7 & 17 & 22 & 2 & 27 & 11 & 16 & 21 & 5 & 26 & 10 & 15 \\ 20 & 4 & 25 & 30 & 13 & 18 & 8 & 23 & 3 & 28 & 14 & 9 & & & & & & \\ \hline \end{array}$ |
| 31 | $\begin{array}{rrrrrrrrrrrrrrrrrr} 1 & 30 & 19 & 14 & 8 & 24 & 29 & 3 & 17 & 12 & 22 & 27 & 2 & 7 & 13 & 18 & 23 & 28 \\ 6 & 11 & 16 & 21 & 26 & 5 & 10 & 31 & 15 & 20 & 25 & 9 & 4 & & & & & \\ \hline \end{array}$ |
| 32 | $\begin{array}{cccccccccccccccccc} 1 & 11 & 6 & 16 & 21 & 26 & 31 & 2 & 12 & 17 & 22 & 32 & 5 & 27 & 15 & 10 & 20 & 4 \\ 25 & 30 & 9 & 19 & 14 & 24 & 29 & 8 & 3 & 18 & 23 & 13 & 28 & 7 & & & & \\ \hline \end{array}$ |
| 33 | $\begin{array}{lccccccccccccccccc} 1 & 6 & 11 & 16 & 21 & 26 & 31 & 5 & 10 & 15 & 25 & 30 & 20 & 3 & 14 & 9 & 33 & 28 \\ 23 & 4 & 18 & 13 & 32 & 27 & 8 & 22 & 17 & 2 & 29 & 12 & 7 & 19 & 24 & & & \\ \hline \end{array}$ |
| 34 | $\begin{array}{llllllllllllllllll} 1 & 28 & 18 & 23 & 8 & 33 & 13 & 3 & 22 & 27 & 32 & 14 & 9 & 19 & 24 & 4 & 34 & 29 \\ 12 & 17 & 2 & 7 & 31 & 26 & 21 & 16 & 11 & 6 & 30 & 25 & 20 & 15 & 5 & 10 & & \\ \hline \end{array}$ |
| 35 | $\begin{array}{rrrrrrrrrrrrrrrrrr} 1 & 28 & 21 & 15 & 34 & 10 & 5 & 20 & 26 & 31 & 14 & 8 & 3 & 25 & 19 & 32 & 12 & 2 \\ 7 & 27 & 17 & 33 & 22 & 9 & 4 & 16 & 29 & 35 & 24 & 11 & 18 & 30 & 6 & 23 & 13 & \\ \hline \end{array}$ |
| 36 | $\begin{array}{lllllllllllllllllll} 1 & 8 & 13 & 23 & 18 & 35 & 30 & 3 & 25 & 20 & 36 & 14 & 31 & 26 & 5 & 21 & 15 & 10 \\ 33 & 28 & 4 & 17 & 9 & 22 & 32 & 27 & 16 & 11 & 6 & 34 & 29 & 19 & 12 & 2 & 24 \\ \mathbf{7} & & & & & & & & & & & & & & & & & \\ \hline \end{array}$ |
| 37 | 32 26 20 14 8 2 33 27 21 15 9 3 34 28 22 16 10 <br> 4 35 29 23 17 11 5 37 31 25 19 13 7 1 36 30 24 <br> 12 6                <br>                  |
| 38 | $\begin{array}{llllllllllllllllll} 8 & 2 & 14 & 20 & 26 & 32 & 38 & 5 & 11 & 17 & 23 & 29 & 35 & 1 & 7 & 13 & 19 & 25 \\ 31 & 37 & 6 & 12 & 18 & 24 & 30 & 36 & 4 & 10 & 16 & 22 & 28 & 34 & 3 & 9 & 15 \end{array}$ |
| 39 | $\begin{array}{rrrrrrrrrrrrrrrrr} 21 & 30 & 36 & 3 & 9 & 15 & 22 & 28 & 34 & 2 & 8 & 14 & 20 & 27 & 33 & 39 & 6 \\ 12 & 18 & 25 & 31 & 37 & 4 & 10 & 16 & 23 & 29 & 35 & 1 & 7 & 13 & 19 & 26 & 32 \\ 38 & 5 & 11 & 17 & 24 & & & & & & & & & & & & \\ \hline \end{array}$ |
| 40 | $\begin{array}{llllllllllllllllll} 9 & 2 & 36 & 30 & 24 & 18 & 12 & 6 & 40 & 34 & 28 & 22 & 16 & 10 & 3 & 39 & 33 & 27 \\ 21 & 15 & 8 & 1 & 35 & 29 & 23 & 17 & 11 & 5 & 37 & 31 & 25 & 19 & 13 & 7 & 38 \\ \hline \end{array}$ |

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|  | $\begin{array}{lllll}32 & 26 & 20 & 14 & 4\end{array}$ |
| :---: | :---: |
| 41 | 5 37 31 13 25 19 7 39 1 33 27 21 15 40 9 34 28 22 <br> 3 16 10 35 41 29 23 17 11 4 36 30 24 18 12 6 38 32 <br> 26 20 14 2 8              |
| 42 | 1 8 40 34 28 22 16 10 4 39 33 27 21 15 9 2 38 32 <br> 26 20 14 7 41 35 29 23 17 3 11 37 31 25 19 5 13  <br> 42 36 30 24 6 12 18            |
| 43 | 5 19 25 39 31 13 7 1 21 41 33 27 12 6 18 42 36 24 <br> 30 10 16 43 37 4 29 23 11 17 38 2 32 26 8 14 20  <br> 40 34 28 3 9 22 15 35           |
| 44 | 6 32 18 12 38 24 4 44 30 17 11 36 5 42 28 22 16 34 <br> 10 40 3 26 20 33 13 39 1 7 23 29 14 41 35 8 21  <br> 27 2 15 43 37 9 31 25 19          |
| 45 | 32 13 38 7 1 25 19 31 43 37 10 3 16 22 28 42 34  <br> 9 15 21 27 44 36 5 11 17 23 29 35 41 8 14 2 26 20 <br> 33 45 39 6 12 24 30 18 40 4         |
| 46 | 1 7 14 32 26 20 41 5 11 35 29 23 17 45 9 38 31 25 <br> 19 44 13 37 6 30 24 43 18 12 3 36 28 42 22 16 8  <br> 2 34 40 27 15 46 21 33 39 4 10        |
| 47 | 9 1 15 31 43 37 7 25 13 19 47 41 5 34 27 14 21 40 <br> 46 8 30 2 24 18 39 45 33 12 6 26 20 44 32 38 3  <br> 11 17 23 29 36 4 10 16 22 28 42 35       |
| 48 | 25 8 1 17 42 36 24 11 30 4 18 44 38 12 32 6 22 <br> 47 41 16 28 34 10 2 48 40 26 20 14 33 7 46 39 27 <br> 19 13 5 45 35 29 23 15 3 43 9 31 21 37    |

[Editor's note: following option is proposed in 1449r1...]
$\underline{f(m, s)}=\{m+13 s\} \bmod L_{\text {pair }, l}$
$g($ PermSeq, $s, m, l, t)=\left\{\operatorname{PermSeq}\left(\{f(m, s)+s+t+l\} \bmod L_{D R U, F P_{i}}\right)+D L_{-}\right.$PermBase $\} \bmod L_{D R U, F P i}$
where

## $\underline{\operatorname{PermSeq}}(k)=k, 0<=k<\underline{L}_{D R U, F P i_{-}}$

and DL_PermBase is an integer ranging from 0 to 31 (TBD), which is set to preamble IDCell or specified by the BCH .
C- $-1,-$

## [Editor's note: following option is proposed in 1450r1...]

Denote the number of LRUs (PRUs) of frequency partition $i$ as $L_{L R U, F P i}$ PRUs, $L_{L R U, F P i}=F P S i * N 2$. The subcarrier permutation is performed in two steps. Step 1 permutes the whole frequency partition into $L_{L R U, F P i}$ virtual distributed LRUs. Note that the number of virtual distributed LRUs equals the number of PRUs in the frequency partition. Step 2 further forms $L_{D R U, F P i}$ distributed LRUs based the $L_{L R U, F P i}$ virtual distributed LRUs.

- Step 1: For each $l$-th OFDMA symbol in the subframe,

1. Allocate the $n_{l}$ pilots within each PRU in the frequency partition as described in section (TBD)
2. Renumber the remaining $L_{L R U, F P i} *\left(P s c-n_{l}\right)$ data subcarriers in order, from 0 to $L_{L R U, F P i}\left(P s c-n_{l}\right)-1$. Group these contiguous and logically renumbered subcarriers into $L_{L R U, F P i} * L_{p a i r, l}$ pairs and renumber them from 0 to $L_{L R U, F P i} * L_{p a i r, l}-1 \ldots$ The renumbered tone pairs in the $l$-th OFDMA symbol are denoted by $R T P_{F P, l, l}$.

Deleted: $f(m, s)=\{m+13 s\} \mathrm{n}$
II
$g($ PermSeq $, s, m, l, t)=\{\{$ Per
II
where II
. $\operatorname{PermSeq}(k, r)$ is is the series
obtained by rotating basic permutation sequence $\operatorname{PermSeq}(k, 0)$ cyclically to the left r times. The basic permutation sequence is defined as II
$\operatorname{PermSeq}(k, 0)=k, 0<=k<L_{D R U, F P i}$ II and $D L_{-}$PermBase is an integer ranging from 0 to 31 (TBD), which is set to preamble IDCell or specified by the BCH. I/
where $k^{\prime}$ is $\bmod \left(\bmod \left(m+s \times 23, L_{\text {pair, },}\right)+l, L_{L R U, F P i}-1\right) ; \operatorname{pair}(s, m, l)$ is the tone-pair index of the $m$-th tone-pair $\left(\left(0<=m<L_{\text {pair, }, l}\right)\right)$ in the $l$-th OFDMA symbol in the $s$-th virtual LDRU; $m$ is the tone-pair index in the $l$-th OFDMA symbol in the $s$-th virtual distributed LRU; $s$ is the virtual LDRU $\left(0<=\mathrm{s}<L_{L R U, F P, i}\right) ; \quad P_{1, c_{1}}(j)$ is the $j$-th element of the sequence obtained by rotating basic permutation sequence $\mathrm{P}_{1}$ cyclically to the left $c_{1}$ times; $P_{2, c_{2}}(j)$ is the $j$-th element of the sequence obtained by rotating basic permutation sequence $P_{2}$ cyclically to the left $c_{2}$ times; $c_{1}=\bmod \left(\mathrm{DL}_{-}\right.$PermBase, $\left.L_{L R U, F P i}\right) ; c_{2}=$ floor (DL_PermBase $\left./ L_{L R U, F P i}\right)$. The operation in [] is over GF $\left(L_{L R U, F P i}\right)$. Specifically, in $\operatorname{GF}\left(2^{\mathrm{n}}\right)$, addition is binary XOR operation. The basic permutation sequences are given in Table 1 t

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## Table 1 - Basic permutation sequences



| 2 | $\mathrm{GF}(2)$ | $\mathrm{P}_{1}$ | 1 |
| :---: | :---: | :---: | :---: |
|  |  | $\mathrm{P}_{2}$ | 1 |
| 4 | $\mathrm{GF}\left(2^{2}\right)$ | $\mathrm{P}_{1}$ | 1,2,3 |
|  |  | $\mathrm{P}_{2}$ | 1,3,2 |
| 8 | $\mathrm{GF}\left(2^{3}\right)$ | $\mathrm{P}_{1}$ | 1,2, 4, 3, 6, 7, 5 |
|  |  | $\mathrm{P}_{2}$ | 1, 4, 6, 5, 2, 3, 7 |
| 16 | $\mathrm{GF}\left(2^{4}\right)$ | $\mathrm{P}_{1}$ | $1,2,4,8,3,6,12,11,5,10,7,14,15,13,9$ |
|  |  | $\mathrm{P}_{2}$ | $1,4,3,12,5,7,15,9,2,8,6,11,10,14,13$ |
| 32 | $\mathrm{GF}\left(2^{5}\right)$ | $\mathrm{P}_{1}$ | $\begin{aligned} & 1,2,4,8,16,5,10,20,13,26,17,7,14,28,29,31,27,19,3,6,12,24,21,15, \\ & 30,25,23,11,22,9,18 \end{aligned}$ |
|  |  | $\mathrm{P}_{2}$ | $\begin{aligned} & 1,4,16,10,13,17,14,29,27,3,12,21,30,23,22,18,2,8,5,20,26,7,28,31 \text {, } \\ & 19,6,24,15,25,11,9 \end{aligned}$ |
| 64 | $\mathrm{GF}\left(2^{6}\right)$ | $\mathrm{P}_{1}$ | $1,2,4,8,16,32,3,6,12,24,48,35,5,10,20,40,19,38,15,30,60,59,53,41$, $17,34,7,14,28,56,51,37,9,18,36,11,22,44,27,54,47,29,58,55,45,25$, $50,39,13,26,52,43,21,42,23,46,31,62,63,61,57,49,33$ |
|  |  | $\mathrm{P}_{2}$ | $1,4,16,3,12,48,5,20,19,15,60,53,17,7,28,51,9,36,22,27,47,58,45,50$, $13,52,21,23,31,63,57,33,2,8,32,6,24,35,10,40,38,30,59,41,34,14,56$, $37,18,11,44,54,29,55,25,39,26,43,42,46,62,61,49$ |

- Step 2: In the virtual distributed LRUs, data tone-pairs from the CRUs are for localized resource. In this step, the localized resources (i.e. the $L_{C R U, F P i}$ PRUs) are "punctured" from the virtual distributed LRUs.

1. Initiate $j=0$.
2. $\quad N^{\prime}=L_{L R U, F P, i}-j$. All the virtual distributed LRUs are numbered 0 to $N^{\prime}-1$. Take out all the data tone-pairs of $\mathrm{CRU}_{\mathrm{FPi}}[j]$ from the virtual distributed LRUs. Then, in the $l$-th OFDMA symbol, there are $L_{\text {pair }, l}$ data tone-pairs punctured from the virtual distributed LRUs.
3. For each $l$-th OFDMA symbol, $l=0,1, \ldots, N_{s y m}-1$,

- Sequentially, take the tone-pairs from the ( $N$ '-1)-th virtual distributed LRUs (Note that "virtual distributed LRUs with index $N$ '-1" is the virtual distributed LRUs with the highest index in all the virtual distributed LRUs) one-by-one and fill them into the $L_{\text {pair }, l}$ punctured tone-pairs (or $L_{\text {pair, } l}-q$ "punctured tone-pairs" if $q$ tone-pairs of the $\left(N^{\prime}-1\right)^{\text {th }}$ virtual distributed LRU belong to $\left.\mathrm{CRU}_{\mathrm{FPi}}[j]\right)$. During the filling process, the largest possible frequency diversity is ensured by the following method:
- Assume an integer variable $x=0,1, \ldots, L_{\text {pair },-}-q-1$. For each $x$, take the $x$-th tone-pair from the ( $N^{\prime}-1$ )-th virtual distributed LRU, and denote the tone-pair as $s_{x}$. Assume that there are $V$ virtual distributed LRUs that have 1 or more data tone-pair punctured. Denote these $V$ virtual distributed LRUs as $c_{v}, v=0,1, \ldots, V-1$. For each $c_{v}$, check how many data subcarriers in $c_{v}$ are from the PRU which $s_{x}$ belongs to, and denote the number as $t_{v}$.
- Find the $1^{\text {st }}$ virtual distributed LRU with the smallest $t_{v}$ among all the $V$ virtual distributed LRUs. Fill tone-pair $s_{x}$ in it.

4. N ' new virtual distributed LRUs are formed. If $j<N_{C R U}-1, j=j+1$, go to b); If $j=N_{C R U}-1$, the
subchannelization for distributed resources are done. The resulted virtual distributed LRUs are $L_{D R U, F P, i}$ distributed LRUs for distributed resource allocation, which are renumbered from 0 to $L_{D R U, F P, i}-1$.
[Editor's note: following option is proposed in 1464r3...]
$f(m, s)=(m+13 \cdot s) \bmod L_{\text {pair }, l}$
$g($ PermSeq $, s, m, l, t)=$ PermSeq $\left[(f(m, s)+107 \cdot l+s) \bmod L_{\text {DRU,.FPi }}\right]$
where PermSeq is the sequence of length $L_{D R U, F P i}$ and is determined by SEED $=\{(I D c e l l+1024 * t) * 1357351\} \bmod 2^{20}$.
The IDcell is the cell identification. The specific permutation sequence generation algorithm with 20-bit SEED ( $\mathrm{S}_{\mathrm{n}-20}, \mathrm{~S}_{\mathrm{n}-19}$, $\left.\ldots, \mathrm{S}_{\mathrm{n}-1}\right)$ and a permutation size of $M$ is defined as below.

The permutation sequence generation algorithm shall generate a permutation sequence of size $M$ by the following process:


```
D. Swap the i-th and the y-th elements in the array (i.e. perform the steps Temp=A[i],\mathbf{A}[i]=\mathbf{A}[y],
        A [y]=Temp).
E. Decrement i by 1.
F. The permuted sequence is represented by PermSeq(i)=A[i].
```


$D_{I P}=\left(\operatorname{Cell~ID~} \bmod \left(L_{D R U, F P i}-1\right)\right)+1$
Deleted: $D_{I P}=($ Cell ID +1$) \mathrm{m}$


Editor's note: following option is proposed in 1448...
$\operatorname{pair}(s, m, l, t)=L_{D R U, F P, i} * f(m, s)+g(\operatorname{PermSeq}(), s, m, l, t), l=0,1, \ldots, N_{s y m}$



```
(4) Generate a lis:: {f(p-2),f(1),f(2),\textrm{L},f(p-3),f(0)}
```

$\qquad$

