# Project
IEEE 802.20 Working Group on Mobile Broadband Wireless Access

**Title**
A Partial Proposal of Rotational OFDM Transmission Scheme

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**Re:**
IEEE 802.20 Working Group Call for Proposals

**Abstract**
As a partial proposal, this contribution discusses the rotational OFDM transmission scheme, which improves spectrum efficiency at the multi-path channel by making use of frequency diversity effect. This scheme can be applied to multi-carrier systems such as OFDMA.

**Purpose**
To propose a new multi-carrier transmission technology which improves the performance of current multi-carrier based technologies. This technology can be applied or merged to complete system proposals based on TDD or FDD.

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**Patent Policy**
1 Introduction

In OFDMA, two types of transmissions are generally considered [1-2]. According to [1], there are called block-wise transmission in localized mode and transmission on non-consecutive (scattered) sub-carriers in distributed mode. The later one makes use of frequency diversity, and is recommended for high speed users and/or delay sensitive traffic.

![OFDMA](image1)

**Figure 1: Distributed mode in OFDMA**

Originally, OFDM has no frequency diversity effect, but in reality, it obtains the frequency diversity effect by use of FEC. This means that, even in distributed mode, the higher the channel coding rate is, the lower the frequency diversity effect becomes. To compensate this weak point, we present the rotational code-multiplexed OFDM with advanced receiver.

2 OFDM Transmission with and without Walsh Code-Multiplexing

2.1 Without Code-Multiplexing

Figure 2 overviews the block diagram for distributed mode, where 2 modulation symbols, A and B, are mapped onto 2 scattered sub-carriers, F1 and F2, respectively. Due to the frequency selective channel, sub-carrier powers are differently received. As a result, there is no frequency diversity effect at the modulation symbols. However, by using the error correction scheme, some frequency diversity is derived, which depends on the coding rate of FEC, though.

![OFDM](image2)

**Figure 2: Normal OFDM in distributed mode.**
2.2 With Walsh Code-Multiplexing

In contrast, OFDM with code-multiplexing, whose diagram is depicted in Figure 3, was expected to obtain the best diversity gain on frequency domain. However, the overall performance with FEC becomes worse than that of OFDM without code-multiplexing mentioned in previous section, because of inter-symbol (or inter-code) interference [3].

![Figure 3: OFDM with Walsh code-multiplexing.](image)

Note that, in Figure 2, WCM means Walsh Code Multiplexing to operate the following formula for 2 dimensions.

\[
\begin{pmatrix} X \\ Y \end{pmatrix} = \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \begin{pmatrix} A \\ B \end{pmatrix}
\]  

(1)

In receiver side, MMSE (Minimum Mean Squared Error) equalization and despreader are used before demodulation.

3 Rotational OFDM Transmission

3.1 Overview

The rotational OFDM transmission is overviewed in Figure 4. There are three features; the rotational code-multiplexer (RCM), multi-dimensional demodulator (MD-DEM) and dual iteration decoder. In the following, those features are introduced briefly in case of QPSK modulation and 2 dimensional code-multiplexing.

![Figure 4: Rotational OFDM (R-OFDM) in distributed mode.](image)

3.2 Features in Rotational OFDM Transmission

3.2.1 Rotational Code-Multiplexer (RCM)

RCM converts modulation symbols, A and B, into sub-carrier symbols X and Y, as follows.
where $\theta_1$ is a rotation angle. If $\theta_1 = 0$, then the signal becomes the same as that of the normal OFDM without code-multiplexing, as mentioned in section 2.1. On the other hand, when $\theta_1 = \pi/4$, the transmission performance is equivalent to that of Walsh code-multiplexed OFDM, as mentioned in section 2.2.

By adjusting the rotation angle, optimum correlation is obtained between modulation symbols A and B, which produces the best frequency diversity. Note that the rotational matrix can be expanded to higher dimensions as follows.

$$
\begin{pmatrix}
X \\
Y 
\end{pmatrix} = R \begin{pmatrix}
A \\
B 
\end{pmatrix} = \begin{pmatrix}
\cos \theta_1 & \sin \theta_1 \\
-\sin \theta_1 & \cos \theta_1
\end{pmatrix} \begin{pmatrix}
A \\
B 
\end{pmatrix}
$$

Let’s assume the QPSK modulation. QPSK symbol consists of I-phase component bit and Q-phase component bit. In this explanation, I-phase bits are paid attention without loss of generality. Let the I-phase bit of modulation symbol A be “a”, and that of symbol B be “b”. Then, the signal constellation constructed by I-phase channels on F1 and F2 is as shown in Figure 4. At the constellation, the minimum distance between signals, such as the distance between “00” and “01”, dominates the transmission performance. Rotating the constellation by $\pi/4$ ($\theta_1 = \pi/4$), makes the minimum distance stable against the Rayleigh fading, due to 2-branch (2-sub-carriers) diversity. However, the diagonal distance, such as in-between “00” and “11”, tends to fluctuate by $\pi/4$ rotation, due to loss of 2-branch diversity. Although the diagonal distance is longer than the minimum distance for 3dB, that drawback is not negligible with FEC. Therefore, optimum rotation angle exists between 0 and $\pi/4$.

3.2.2 Multi-Dimensional Demodulator (MD-DEM)

Because of the frequency selectivity, signal constellation of Figure 5 is generally distorted as shown in Figure 6. The conventional receiver uses MMSE equalization and despreading, as shown in Figure 3, which brings inter-symbol (or inter-code) interference (ISI). To avoid the ISI, multi-dimensional demodulator is used here, detecting the likelihood of the code-multiplexed symbol, as shown in Figure 6.
3.2.3 Dual Iteration Decoder (Twin Turbo Decoder)

In general, MAP decoding assumes no correlation between inputted soft decisions as well as Viterbi decoding. Therefore, for correlated signals, their mutual information is discarded in conventional decoder. In order to take it in, Twin Turbo Decoder [4] seems appropriate for this rotational OFDM. Figure 7 shows the overview of the twin turbo decoder. In addition to the conventional feedback loop for “Brief Propagation”, there is a 2nd feedback loop for “Brief Coupling”. In this decoder, soft decisions are updated during Turbo decoding.

![Diagram of Twin Turbo Decoder](image)

Figure 7: Twin Turbo Decoder.

3.3 Performance Evaluation

3.3.1 Simulation Assumption

Table 1 lists the simulation parameters. In this simulation, one user frame occupies whole sub-carriers. Code-multiplexed symbols (X and Y in Figure 4) are randomly assigned to sub-carriers. For Walsh code-multiplexed OFDM, the desbreaker with MMSE equalizer was assumed.
Table 1. Simulation Parameters

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Occupied Bandwidth $W$</td>
<td>5.0 MHz</td>
</tr>
<tr>
<td>Sampling rate $t_s$ ($= 1 / W$)</td>
<td>0.2 µsec.</td>
</tr>
<tr>
<td># of sub-carriers</td>
<td>512</td>
</tr>
<tr>
<td>Data symbol duration</td>
<td>102.4 µsec.</td>
</tr>
<tr>
<td>CP duration</td>
<td>11.2 µsec.</td>
</tr>
<tr>
<td># of info. bits / frame (incl. tail bits)</td>
<td>1024 ($R = 1/2$), 3072 ($R = 3/4$)</td>
</tr>
<tr>
<td>Frame length</td>
<td>1 OFDM symbol ($R = 1/2$ &amp; 16QAM), 2 OFDM symbols ($R = 1/2$ &amp; QPSK, $R = 3/4$ &amp; 16QAM), 4 OFDM symbols ($R = 3/4$ &amp; QPSK)</td>
</tr>
<tr>
<td>Channel coding</td>
<td>Turbo code ($K = 4$)</td>
</tr>
<tr>
<td>Decoding algorithm</td>
<td>Max Log-MAP / 8 iterations</td>
</tr>
<tr>
<td>Modulation</td>
<td>QPSK, 16QAM</td>
</tr>
<tr>
<td>Rotation dimension ($= D$)</td>
<td>2, 4</td>
</tr>
<tr>
<td>Rotation angle for rotational OFDM</td>
<td>$\theta_1, \theta_2 = 0.3 \sim 0.7 \pi/4$</td>
</tr>
<tr>
<td>Channel model</td>
<td>Pedestrian B (3 km/h), Vehicular B (30 km/h) [6]</td>
</tr>
<tr>
<td># of receiving antenna</td>
<td>1</td>
</tr>
<tr>
<td>Channel estimation</td>
<td>Ideal</td>
</tr>
</tbody>
</table>

3.3.2 Simulation Results

In this simulation, 2 kinds of OFDM transmission are taken into account for distributed mode. As normal OFDM transmissions, there are no code-multiplexing OFDM mentioned in section 2.1. For the rotational OFDM transmission scheme, 2 dimensions and 4 dimensions were assumed. Figure 8 and 9 compare the FER performances among 2 OFDM schemes in case of QPSK modulation. When the coding rate is higher, rotational OFDM becomes better than normal ones. Figure 10 and 11 are for 16QAM cases. Although the gain of rotational OFDM scheme decreases, significant gains have been confirmed.

4 Conclusion

In this contribution, we presented a rotational OFDM transmission scheme for distributed mode. By using the RCM (Rotational Code Multiplexing) and advanced detection, frequency diversity gain increases, especially in case of higher channel coding rate. It should also be noted that the RCM is a parameterized function which contains normal OFDM scheme with no rotation angle. With this scheme, spectrum efficiency can be significantly improved for distributed mode in OFDMA.
Figure 8: Frame Error Rates (QPSK in Pedestrian B channel).

Figure 9: Frame Error Rates (QPSK in Vehicular B channel).
Figure 10: Frame Error Rates (16QAM in Pedestrian B channel).

Figure 11: Frame Error Rates (16QAM in Vehicular B channel).
References


