

TDEC for PAM4

Potential TDP replacement for clause 123,
and Tx quality metric for future 56G PAM4 shortwave
systems

802.3bs ad hoc

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Introduction

- Link budgets close if:
 - Tx eye quality and SRS test source calibration metrics use equivalent methods
 - The Tx eye quality metric yields a dB value which correlates with the system penalty of real transmitters
- Two broad options
 - TDP
 - hardware based sensitivity measurement comparison
 - needs definition of a hardware reference Rx and reference equalizer
 - and live with the knowledge that everyone will have a slightly different implementation of these which may lead to interoperability issues and variability in practice

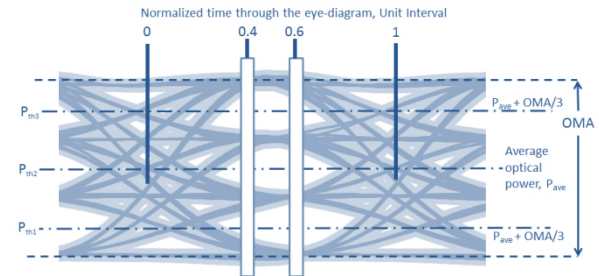
or

- TDEC
 - A real time or sampling 'scope based measurement; real time 'scope is probably easier to standardize; sampling 'scope probably more likely to be used in practice.
 - Requires a short test pattern ($< 2^{16}$ bits), definition of software based reference Rx and reference EQ, post processing using either an error counting or partial error probability calculation on the pattern or a reconstructed eye
- This presentation looks at a 'scope based metric

Proposal for TDEC for PAM4 signals -1

- Scope based, TDEC variant expanded for all three sub-eyes in equalized PAM4 signal

- No reference Tx needed
- Worst case fibre required for SMF
- Reduced bandwidth (19.6 GHz BT4) Rx for MMF



- Reference receiver and equalizer are software based 'in the 'scope'
- **Single timing position in centre of eye for all three sub-eyes, +/-0.1 UI (TBC)**
 - Time centre of eye determined from crossing points
- **TDEC calculated from fixed thresholds:** P_{ave} , $P_{ave} + OMA/3$, $P_{ave} - OMA/3$
 - Penalizes transmitters which have unequal sub-eyes
 - This isn't how a 'real' PAM4 retimer is expected to work, but it avoids the issue of how to measure accurately the penalty of unequal sub-eyes when received by a 'real' receiver, which may have differing sensitivities for each sub-eye.
 - Part of the motivation for this work is to evaluate how much penalty that may incur
 - Should 400GE decide that optimized thresholds ought to be specified for the TDEC test, an additional (non-trivial) test will be needed to measure how transmitter and receiver sub-eye inequality/non-linearity interact.

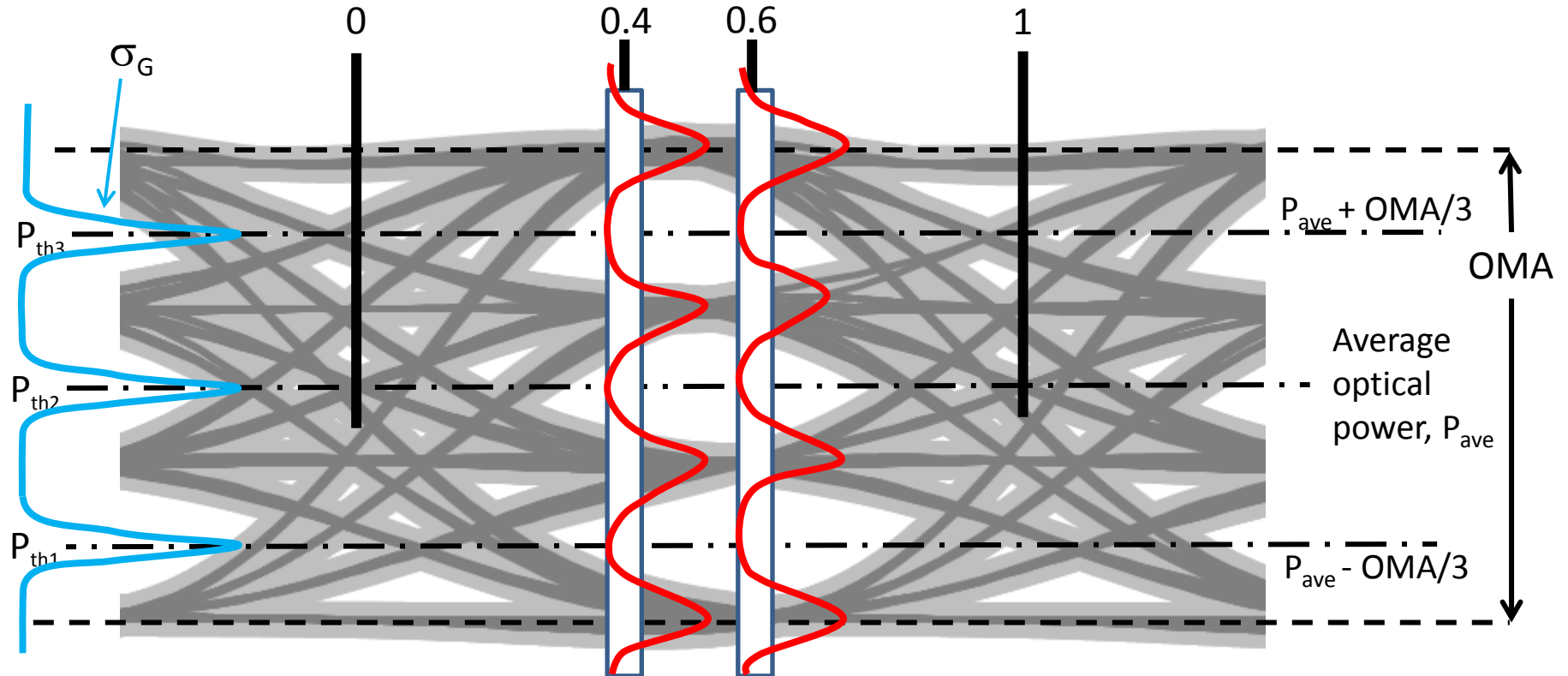
Proposal for TDEC for PAM4 signals -2

- Conceptual basics
 - Measure the combined O/E and 'scope noise without signal, σ_{OE}
 - Measure histogram through equalized eye to be tested, normalize
 - Equalization is done in the 'scope with a ref. equalizer (eg 5 T/2 tap FFE)
 - A sampling 'scope would need to do the equivalent of: measure the noise on the unequalized pattern, capture the averaged pattern and equalize it, and add back in a noise term which is consistent with the noise frequency spectrum and equalization applied
 - The histogram is a vector representing the vertical probability density function (PDF) through the PAM4 eye
 - Do this for left and right of eye time centre
 - From the vertical PDF through the PAM4 eye, create 3 cumulative probability functions, one around each sub-eye threshold.
 - Add normalized Gaussian noise term σ_G to the sub-eye thresholds
 - to create 3 PDFs consisting of a Gaussian PDF centred around each of the sub-eye thresholds
 - Multiply each threshold PDF by the appropriate cum've eye PDF to calculate a proxy for SER for that threshold; sum the results
 - Find smallest size of σ_G that makes resultant = target SER = 3.2×10^{-4}
 - Root sum square the 'scope noise to σ_G *see note*
 - Find the equivalent σ_{ideal} for an ideal PAM4 signal: $\sigma_{ideal} = \frac{OMA}{6Qt}$
 - TDEC is the dB ratio of σ_{ideal} and $(\sigma_G^2 + \sigma_{OE}^2)^{1/2}$ *see note*

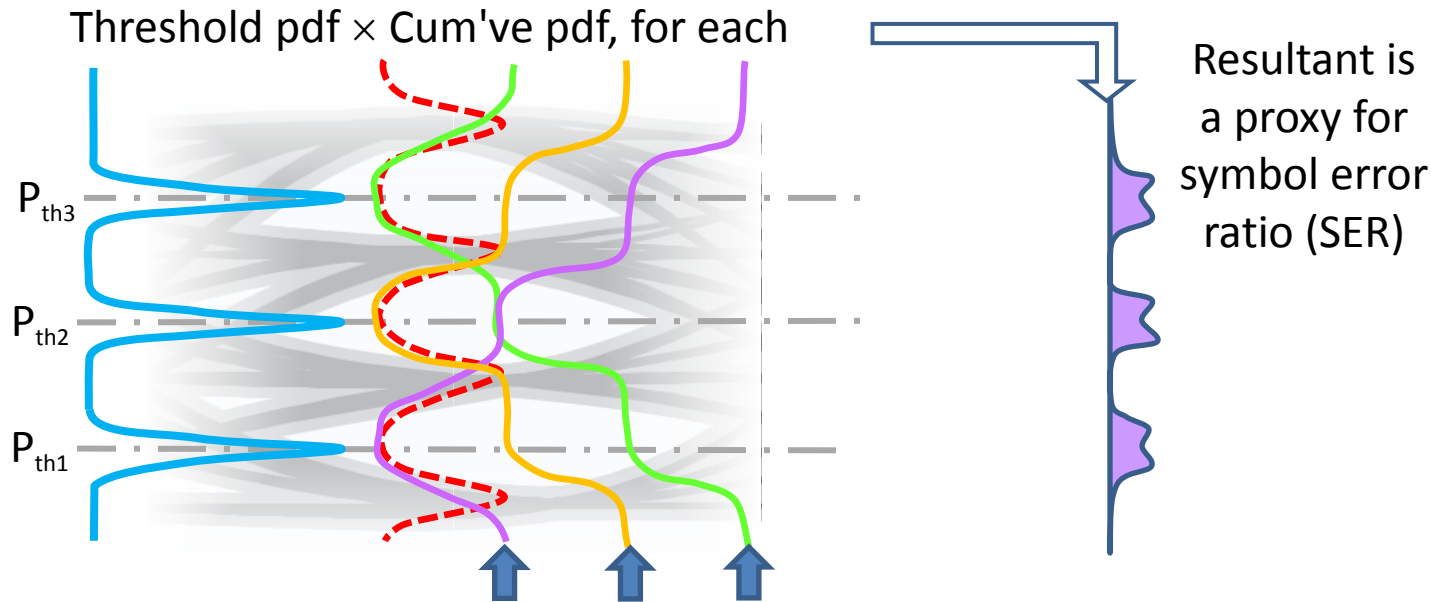
Note: additional manipulation of σ_G is needed to account for noise filtering by the EQ

Test Method: Two histograms

Normalized time through the eye-diagram, Unit Interval



Processing, for each histogram through the eye



- Create three cumulative probability functions, one around each threshold
- Find the smallest value of σ_G to make SER = target SER
- Borrowing from 100GBASE-SR4, the noise, R, that could be added by a receiver is:

$$R = (1-M_1) \cdot [\sigma_G^2 + \sigma_{OE}^2 - M_2^2]^{1/2} \quad \text{equation (1)}$$

where M_1 and M_2 account for mode partition noise and modal noise (both are zero for SMF applications), and σ_{OE} is the rms noise of the O/E and scope combination.

- TDEC is given by:

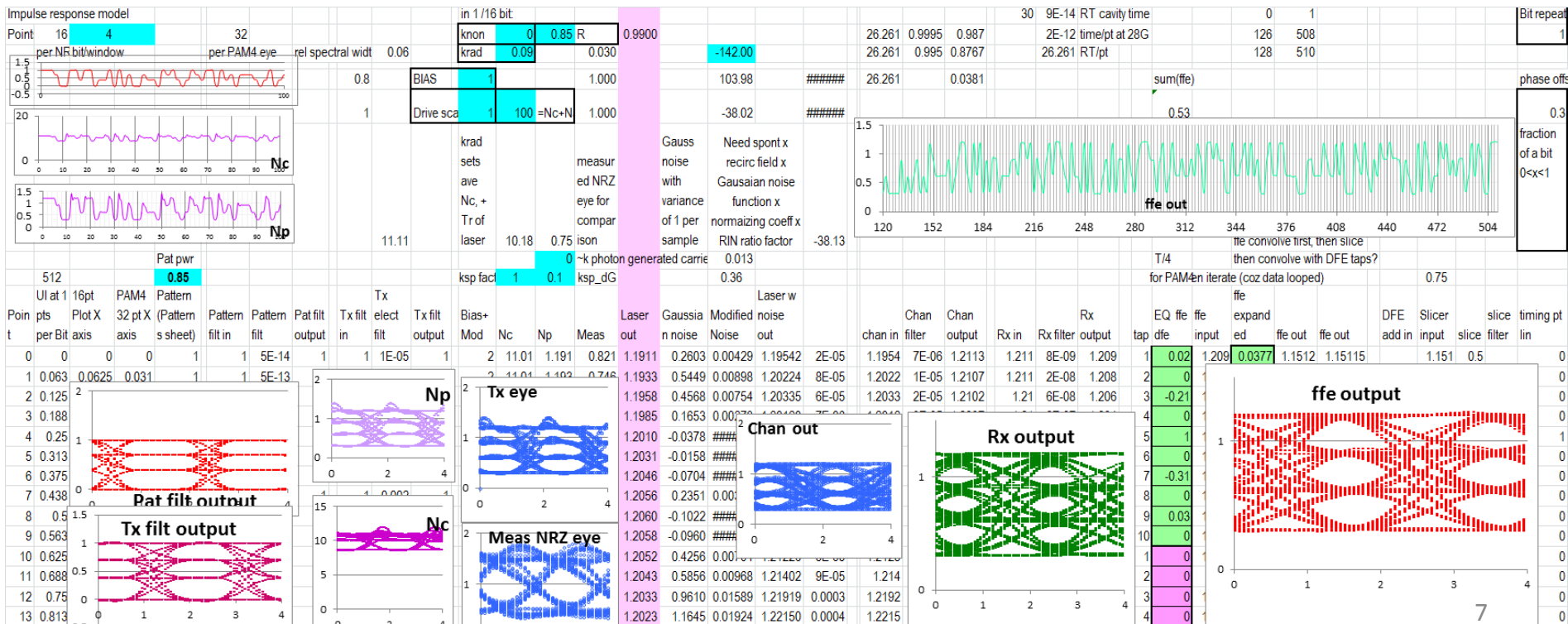
$$\text{TDEC} = 10 \cdot \log_{10} \left(\frac{OMA}{6} \times \frac{1}{Q_t R} \right) \quad \text{equation (2)}$$

where Q_t is the Q function value consistent with the target symbol error ratio

- The largest TDEC value, calculated for either left or right histogram, is used

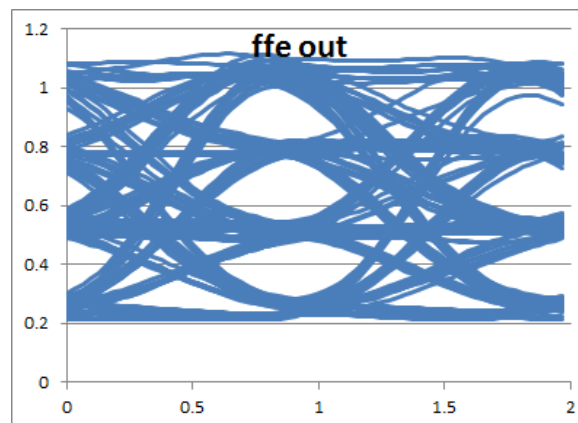
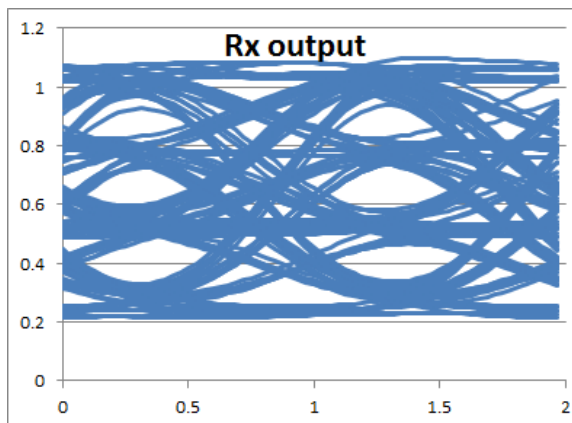
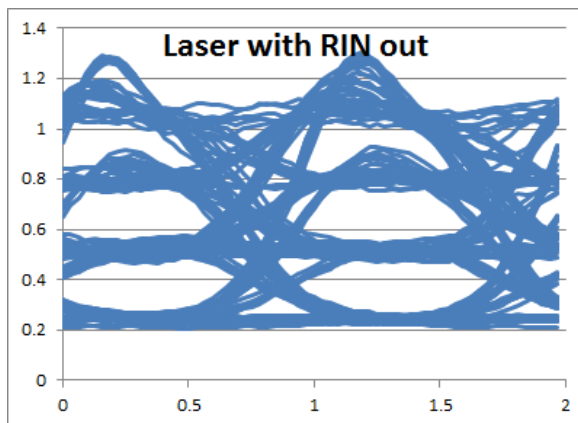
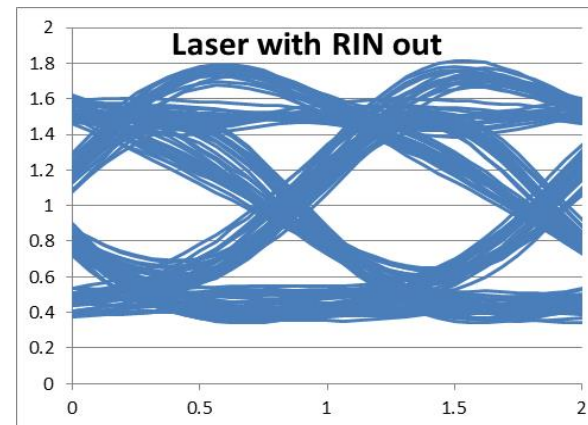
Model to emulate eyes and calculate TDEC

- Dimensionless impulse response based spreadsheet model
 - quasi 'rate equation' laser, with RIN (to produce life-like waveforms)
 - PAM4 data from sequential pairs of bits from a PRBS9 pattern
 - Expanded to 32 samples per bit period
 - Gaussian channel and Rx bandwidths, 5 tap T/2 FFE
 - Output eyes from laser, Rx and FFE
 - Vertical histograms through eye (256 points per time slice per noise instance)
 - 16 noise instances used to build statistics for TDEC calculations

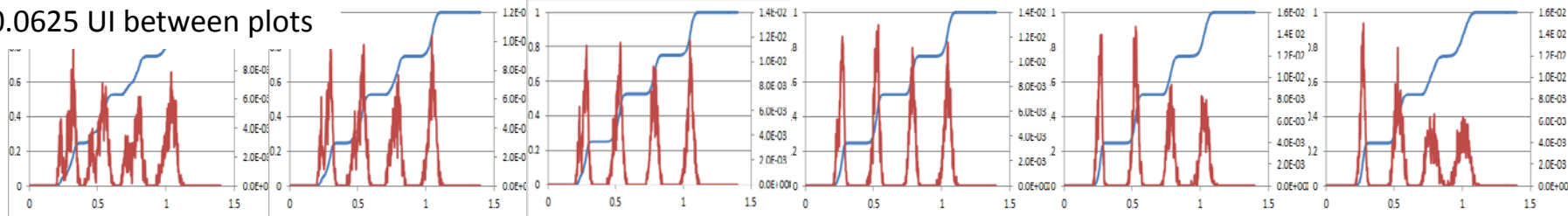


Modeling output: nominal Tx

- Eyes and eye histograms based on a modelled laser with performance similar to a moderately fast 25G laser at high temperature
 - The NRZ eye for the same VCSEL model is very similar to a typical measured 26G VCSEL eye (RHS)



0.0625 UI between plots



Eyes and eye histograms for a moderately fast 25G VCSEL

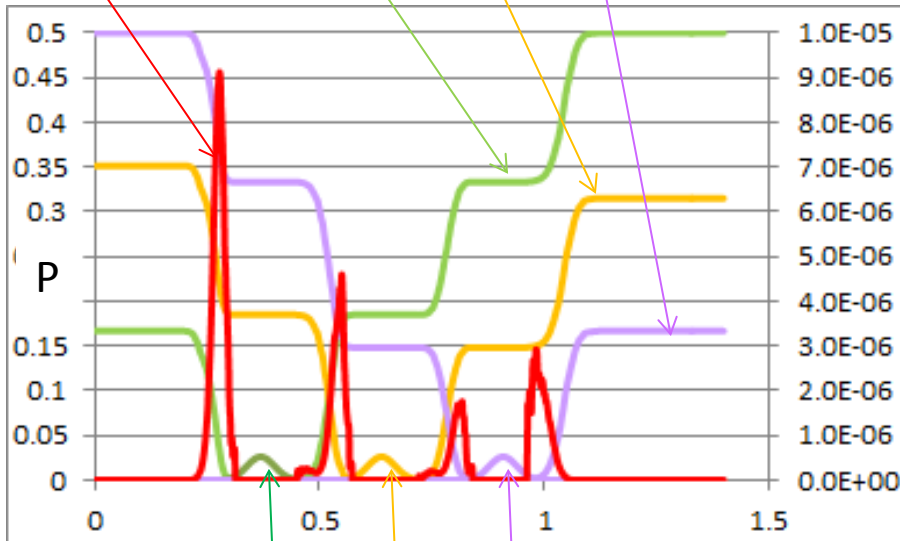
The NRZ eye for the same VCSEL model is similar to typical 26G VCSEL at high temp

TDEC vs time through eye (nominal speed laser)

(nominal speed laser)

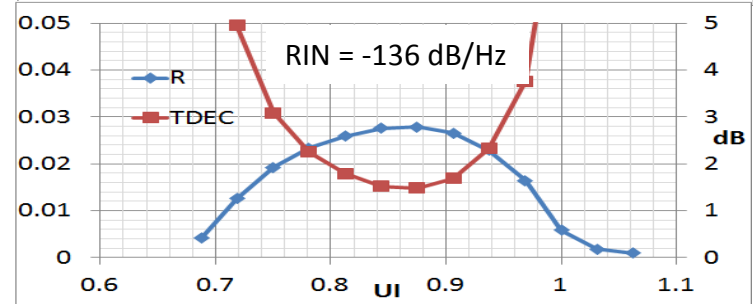
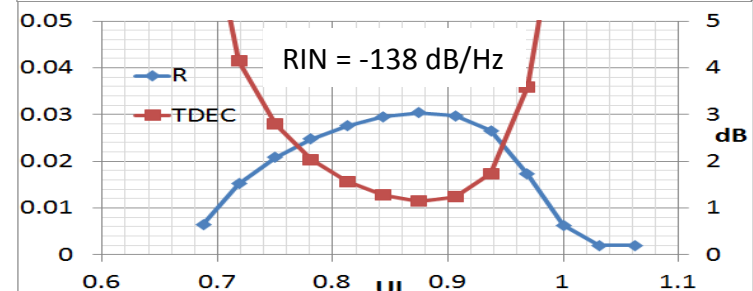
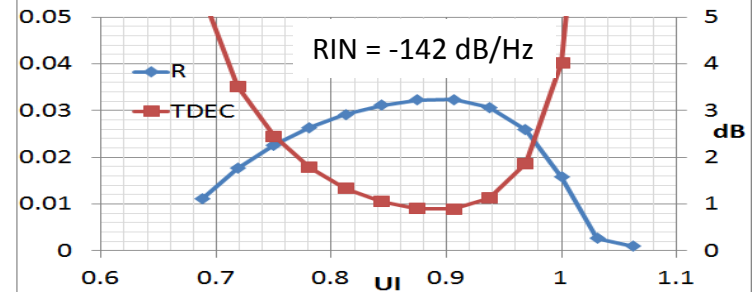
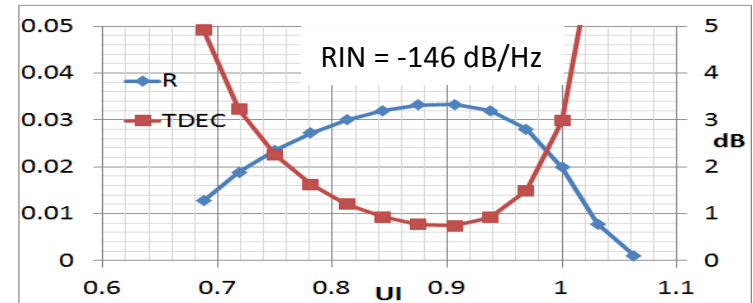
'error probability'

cumulative probability plots
through eye, centered
around each threshold



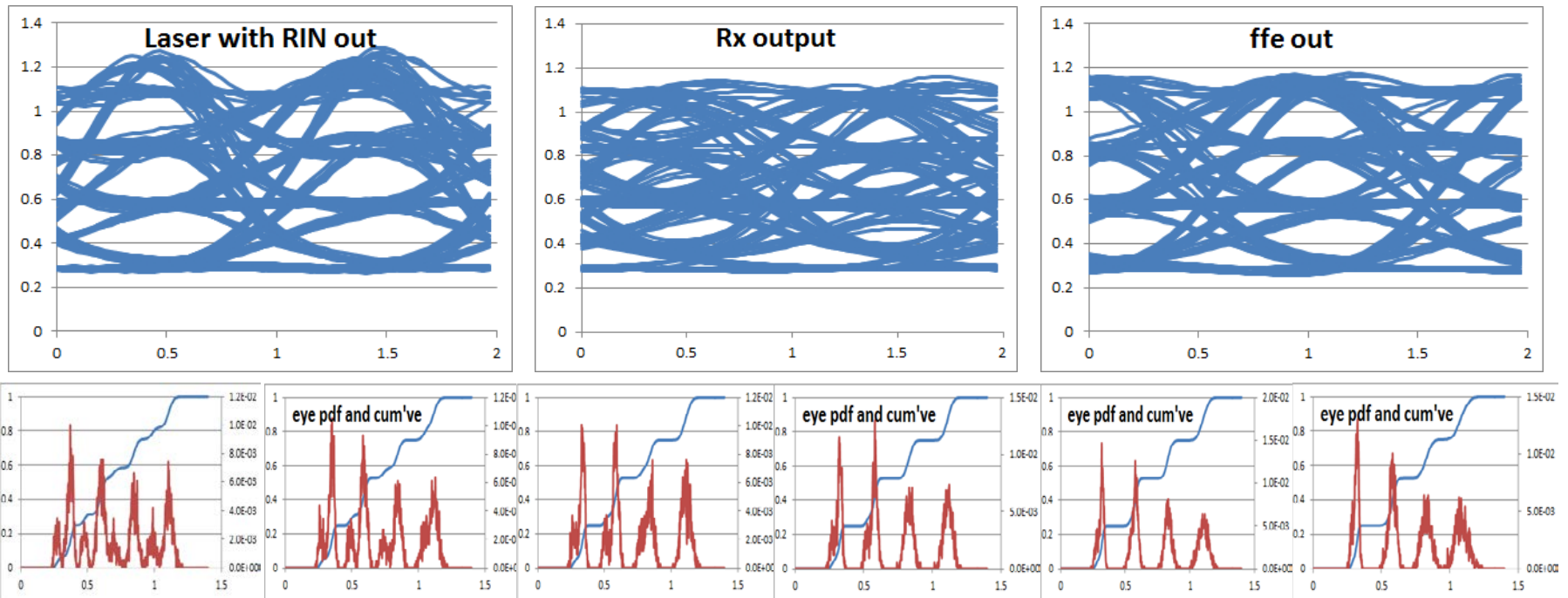
pdf of noise broadened thresholds

- TDEC ~ 1 dB at centre of eye
- TDEC ~ 2.5 dB at ± 0.1 UI



Modeling output: slow Tx

- Slower laser

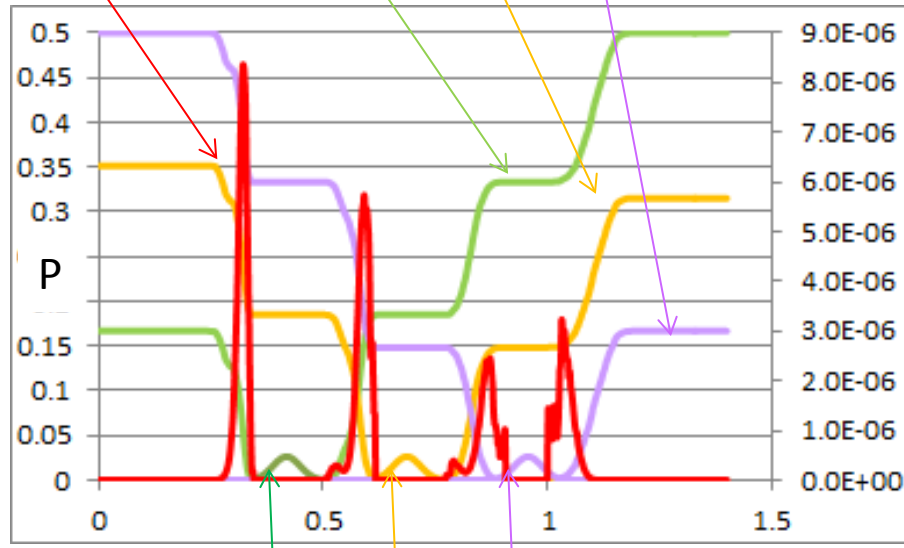


Eyes and eye histograms for a slow 25G VCSEL.

TDEC vs time through eye (low speed laser)

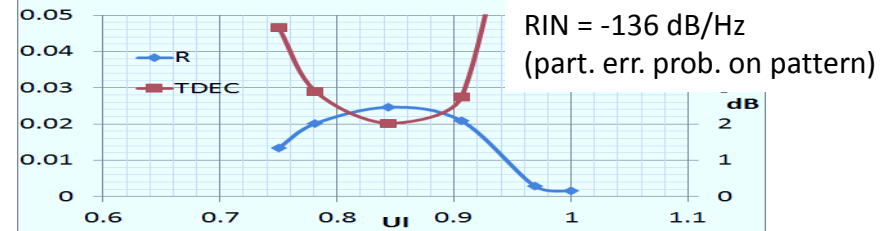
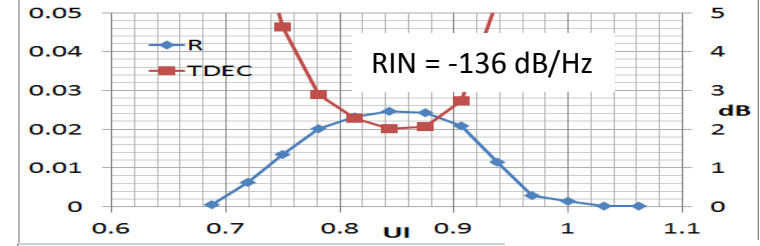
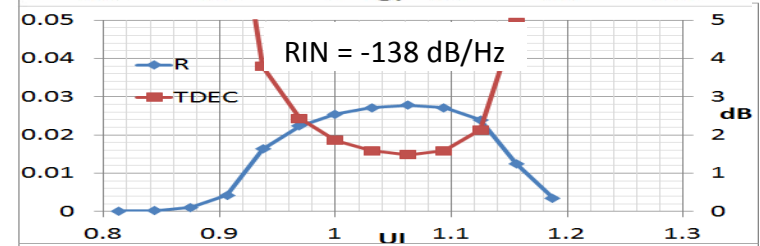
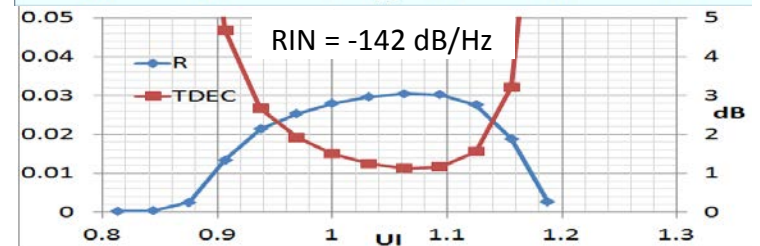
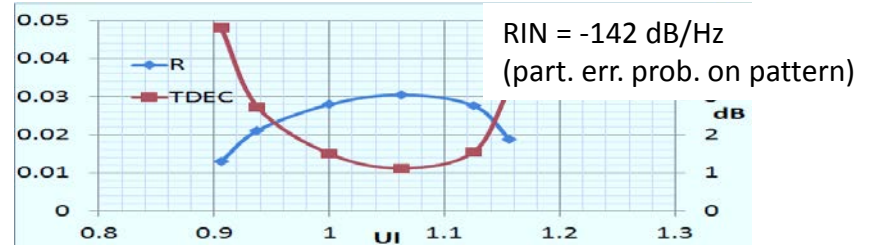
cumulative probability plots
through eye, centered
around each threshold

'error
probability'



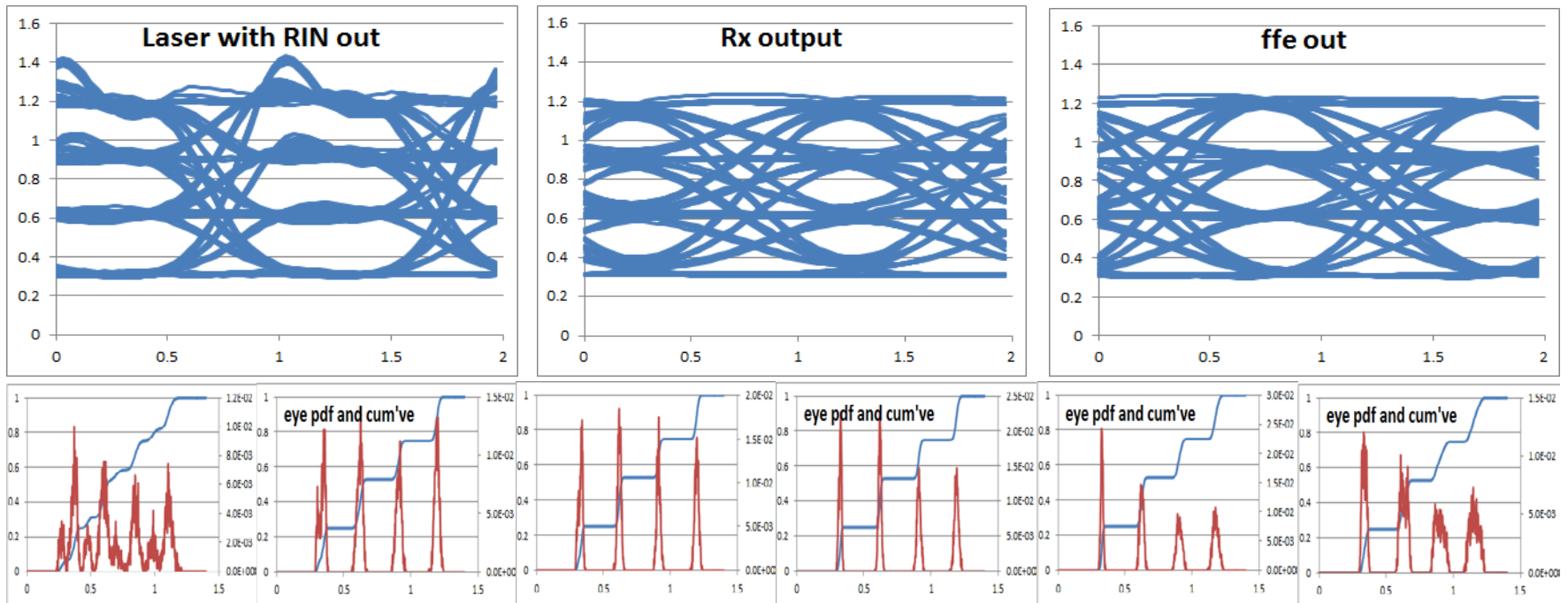
pdf of noise broadened thresholds

- TDEC \sim 1-2 dB at centre of eye
- TDEC $>$ 5 dB at \pm 0.1 UI



Modeling output: fast Tx

- Faster laser



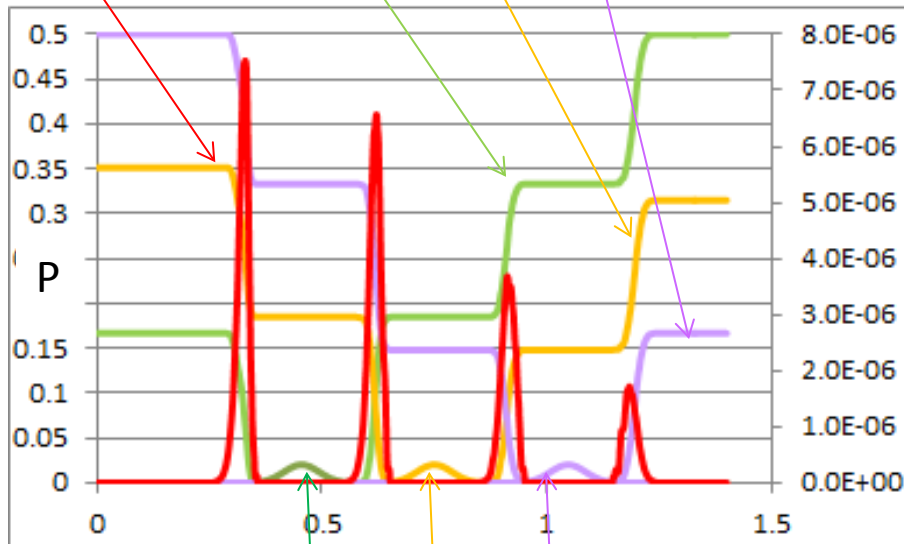
Eyes and eye histograms for a fast 25G VCSEL.

TDEC vs time through eye

(fast laser)

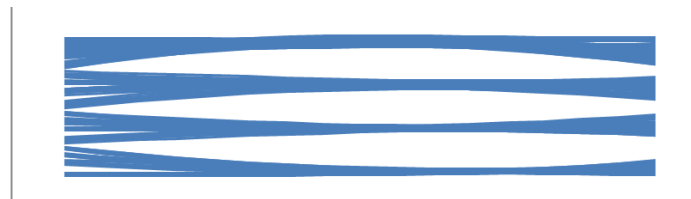
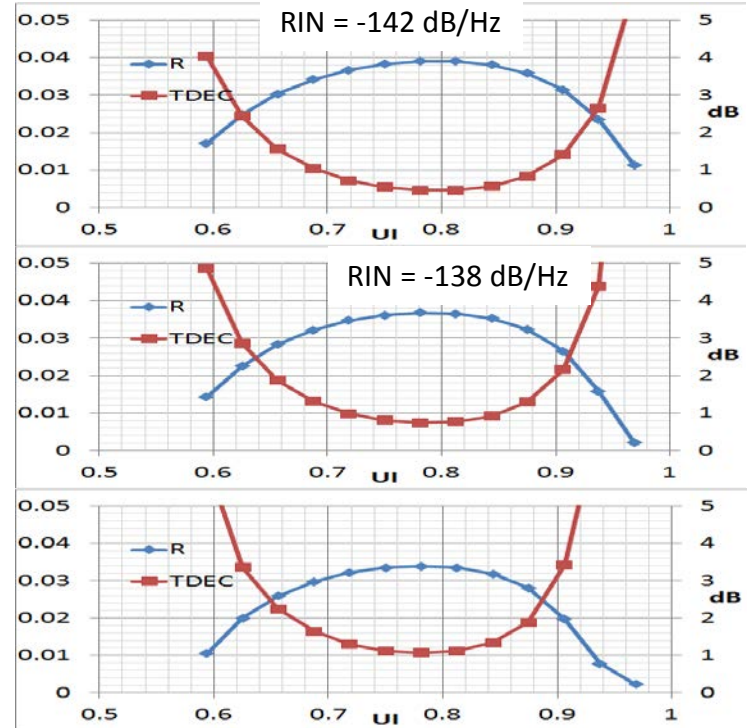
'error probability'

cumulative probability plots through eye, centered around each threshold



pdf of noise broadened thresholds

- TDEC ~ 0.5 dB at centre of eye
- TDEC ~ 1 dB at ± 0.1 UI



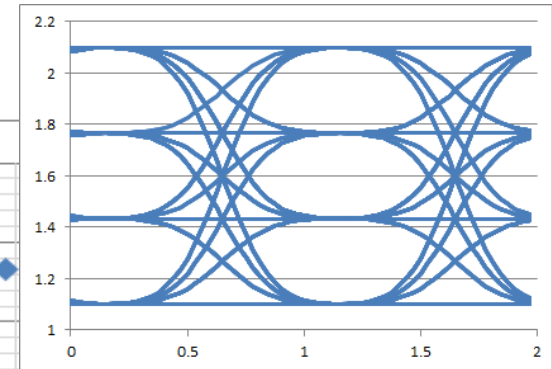
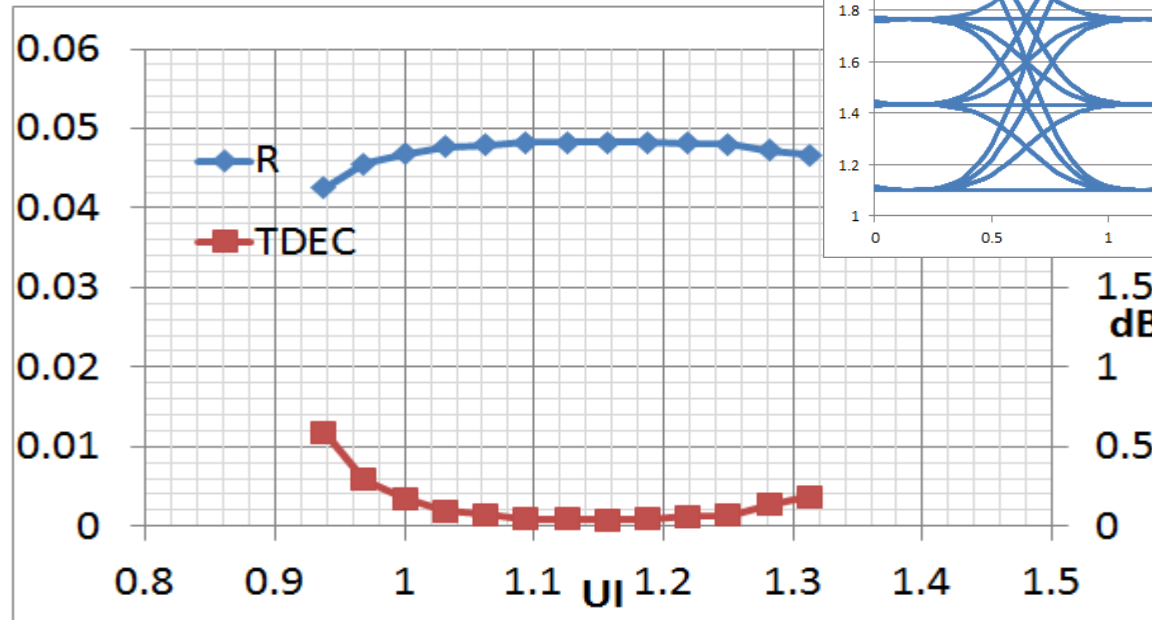
Further work

- Check the math's, and noise treatment
 - and write out how to treat the noise when capturing the transmitter pattern, and when adding noise to thresholds when calculating TDEC
- TDEC time sampling points
 - +/- 0.1 UI timing offset is probably too large and may represent an unrealistically large Tx penalty
 - to be reviewed in light of real PAM4 CDR data
 - E.g. a PAM4 CDR with +/-1.25 ps timing error from centre of eye, and 0.18 ps RJ, would suggest +/-0.05 UI timing offset should be used
- TDEC validation
 - show good correlation between TDEC and system sensitivity measurements with reference receiver
 - and show good correlation between TDEC and system simulations
 - TDEC calculated by histogram and pattern methods are identical
 - 0 dB TDEC achieved at centre of clean eye; Value of σ_G for 0dB TDEC consistent with PAM4 modulation penalty and target SER

Appendix A: TDEC validation

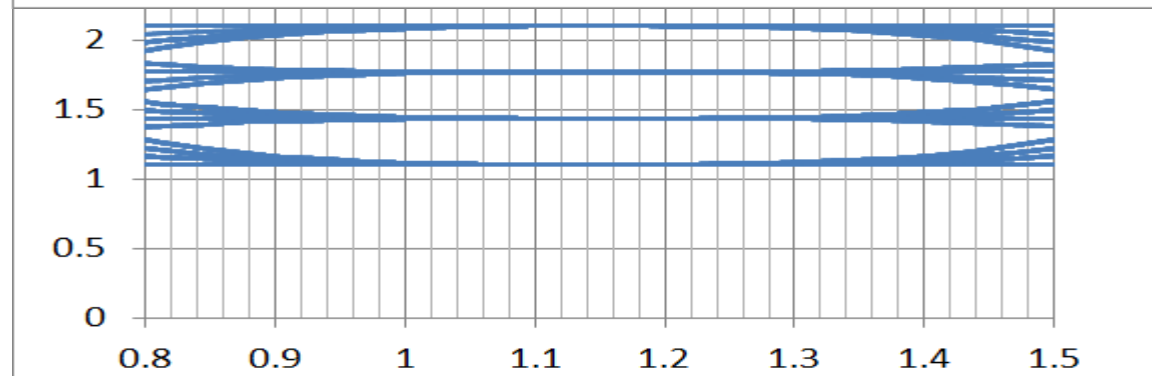
- 0 dB TDEC at the centre of an ideal eye

Max R = 0.0484



$$OMA_{\text{inner}} = 1/3$$

$$OMA_{\text{inner}}/(2R) = 3.44$$



Appendix B: Notes on noise treatment

- Noise is effectively added at the receiver to calculate TDEC
- Since the Rx precedes the EQ, the noise density vs frequency matters. Assuming an FFE implementation for simplicity:
 - Typically, the FFE is boosting high frequencies to open the eye
 - high frequency noise is increased by the FFE
 - if the noise term present at each tap is uncorrelated, the relative noise amplitude increases as the RSS of the tap ratios (typically >1)
 - low frequency noise is reduced
 - if the noise terms at the taps are correlated, the relative noise amplitude increases as the sum of the tap ratios (typically < 1)
 - for TDEC calculations, the frequency content of the noise after the EQ is not important, but the amplitude of the noise is
 - Maybe assuming pink noise which is uncorrelated at each FFE tap is a reasonable starting point ...

Changes needed to incorporate TDEC into clause 123

- *work in progress – to be presented separately*