

# Elevated NEV Due to Triplen Harmonics



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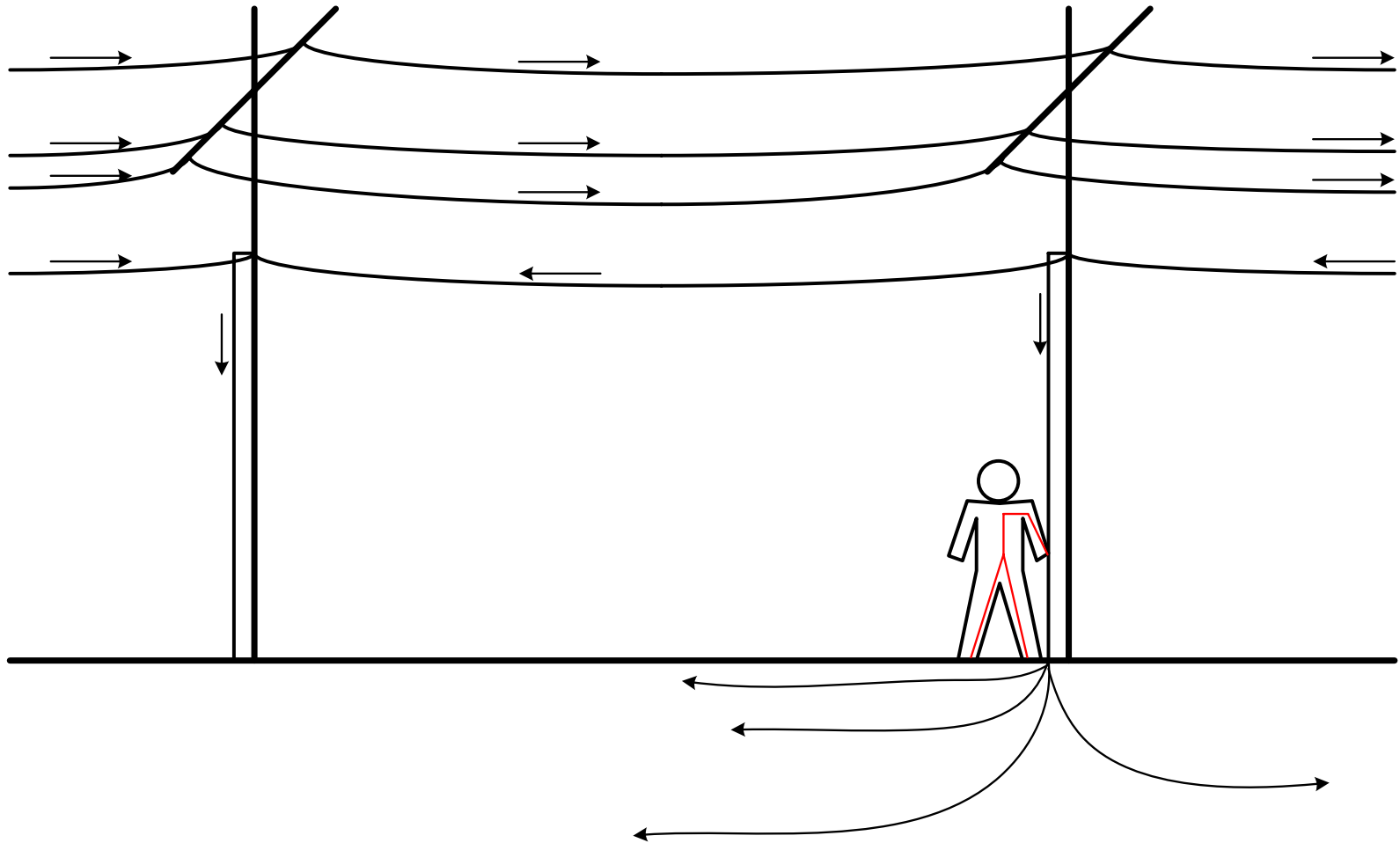
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Panel Session PN-29 Stray Voltage: Causes, Impacts and Mitigation

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# Neutral-to-Earth Voltage



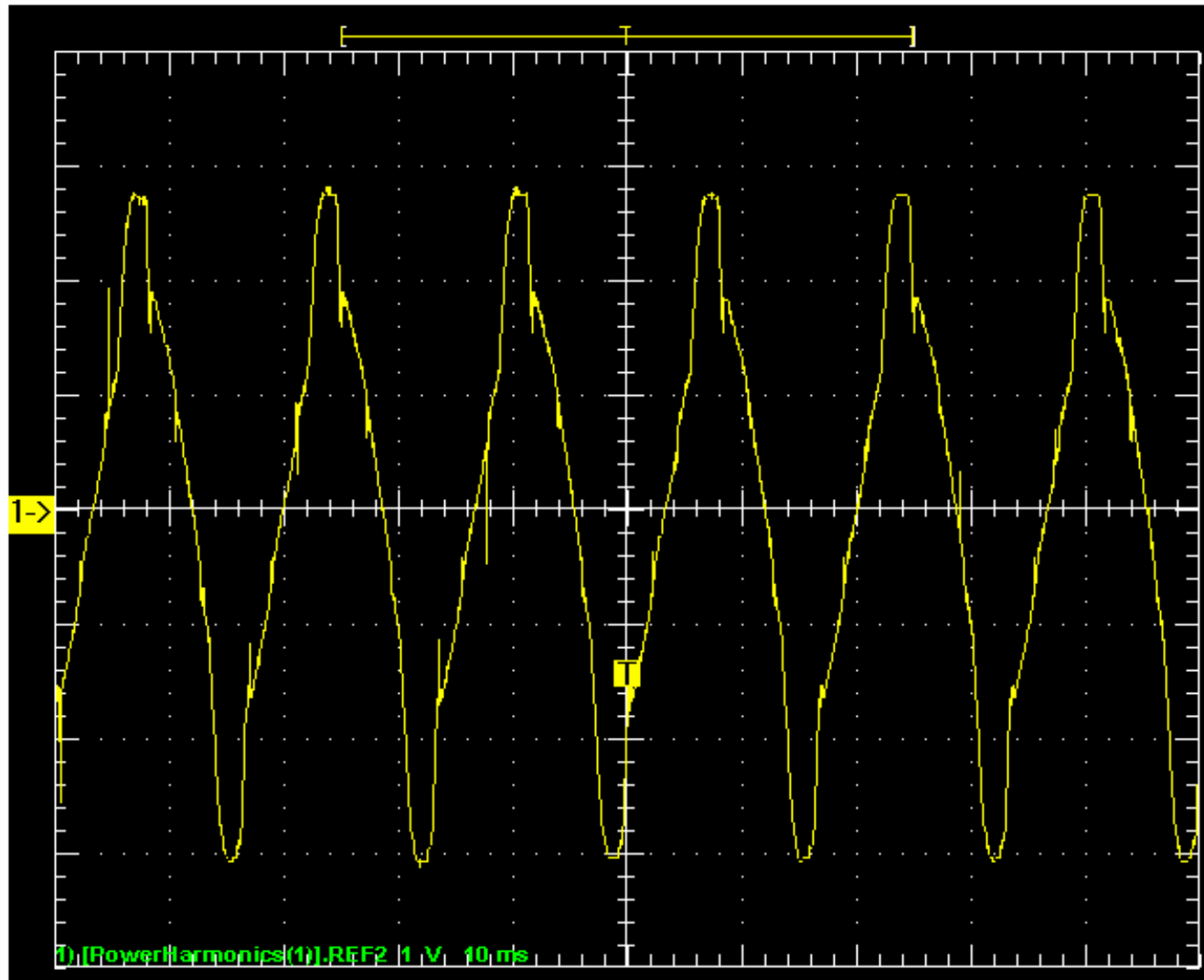


# Factors Affecting NEV

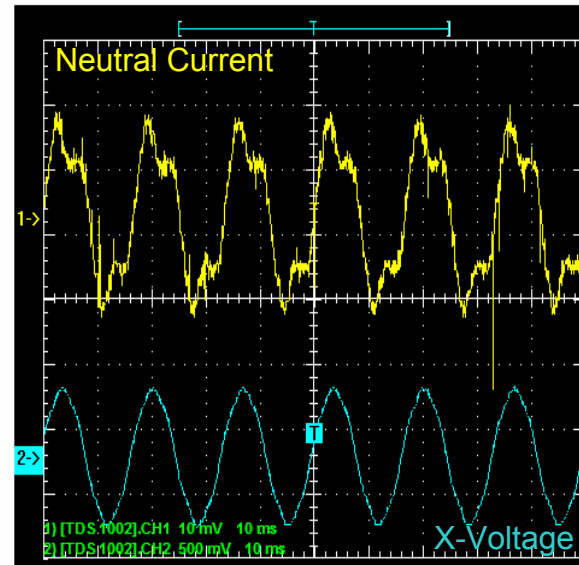
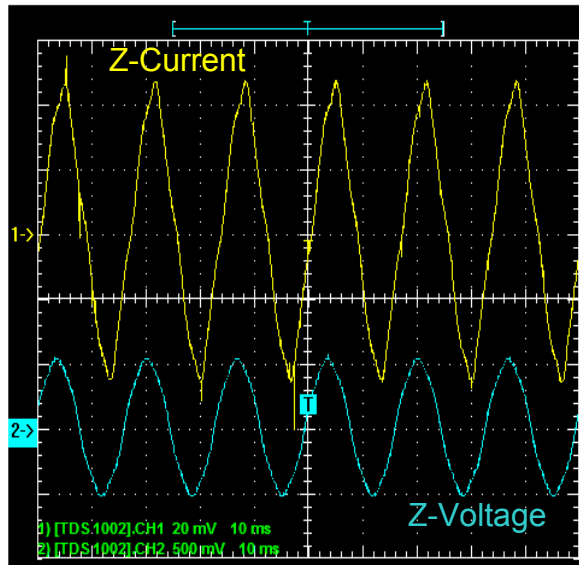
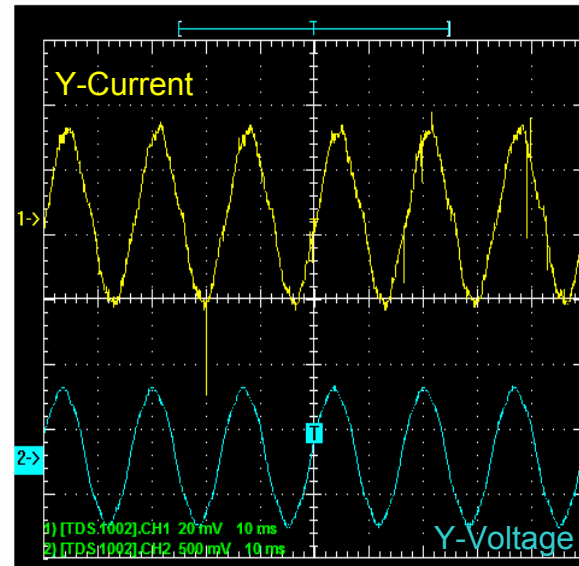
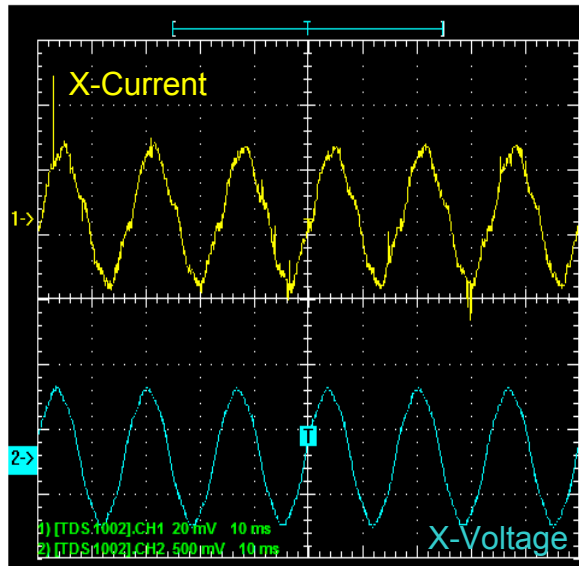
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- Power system grounding
- Load balancing
- Transformer connection
- Primary circuit voltage level
- Neutral conductor impedance
- Neighboring ground fault
- Parallel utilities with common bonds

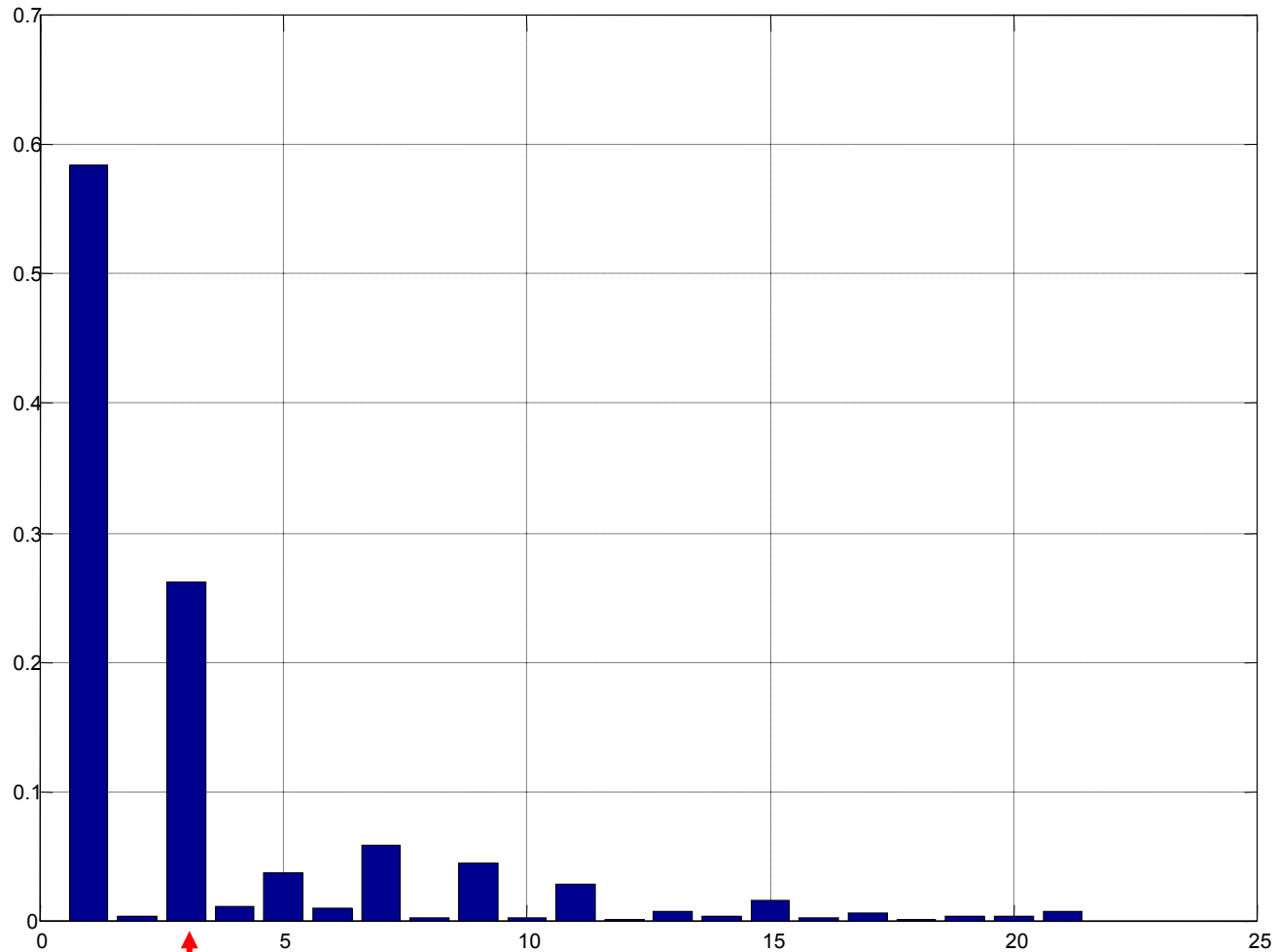
# NEV at Three-Phase Pole



# Distribution Feeder Measurements



# NEV Spectrum



Third Harmonic is 40% of the Fundamental



# Non-Linear Loads and Their Impact on NEV

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- Proliferation of single phase nonlinear residential loads
  - Rectifiers/Power Electronics
  - Magnetics (e.g., single-phase motors)
- Increased triplen harmonic distortion
- Elevated neutral conductor current
- Interference with capacitors and harmonic filters

# Some typical loads drawing 3<sup>rd</sup> harmonic currents



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- Rectifiers

- Power supplies in all consumer electronics, motor drives, lighting, etc.

- Single-phase induction motors

- Used in almost every motorized application in with single-phase service: Compressors (HVAC, Freezers, Refrigerators), Fans, Pumps, Washers and dryers, etc.
- Several types: Cap start, Cap-start and run, Split-phase, Shaded pole

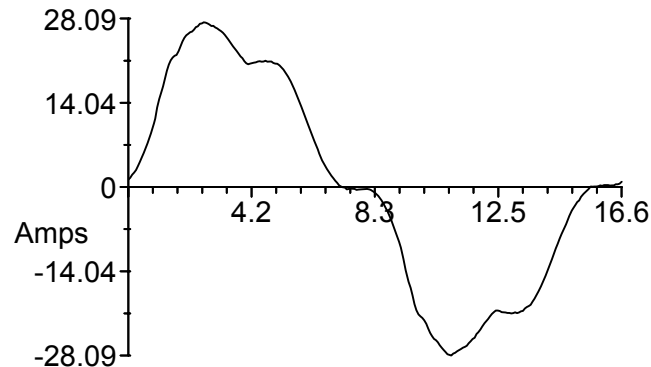


# Residential Load: *L1*

Event: 150 Of 425  
Duration: 1 Cycles

Event Triggered by Time  
Event Trigger Cycle 1

Time: 09/25/2004 09:38:49.000  
Input: Ia Amps  
Cycle: 1

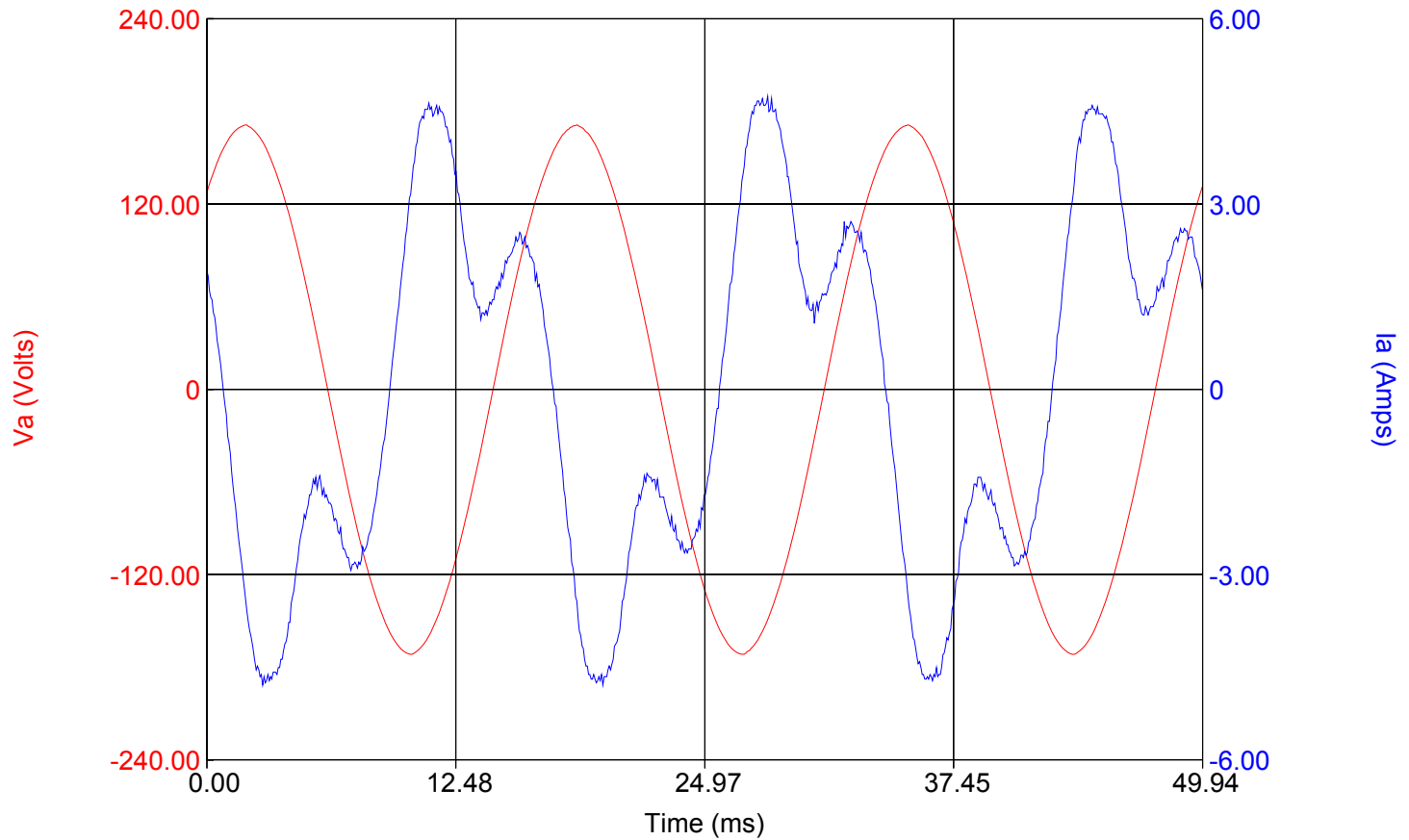


Cycle Waveform

Total Harmonic Distortion	19.52 %
Odd Contribution	19.52 %
Even Contribution	0.51 %
RMS Of Fundamental	17.13 A
RMS Of Fund + Harm	17.45 A
K Factor	1.75

Harm Fund	% Of Fund	Amps	Angle	Harm	% Of Fund	Amps	Angle
2	0.19	0.0	129°				
3	12.78	2.2	211°				
4	0.33	0.1	319°				
5	14.42	2.5	147°				
6	0.12	0.0	297°				
7	1.92	0.3	189°				
8	0.14	0.0	55°				
9	1.93	0.3	38°				
10	0.12	0.0	270°				
11	0.67	0.1	281°				
12	0.13	0.0	152°				
13	0.43	0.1	228°				
14	0.07	0.0	15°				
15	0.76	0.1	132°				
16	0.10	0.0	194°				
17	0.57	0.1	6°				
18	0.04	0.0	68°				
19	0.16	0.0	312°				
20	0.06	0.0	342°				
21	0.32	0.1	235°				
22	0.05	0.0	174°				
23	0.17	0.0	155°				
24	0.04	0.0	55°				
25	0.16	0.0	70°				
26	0.03	0.0	292°				
27	0.34	0.1	293°				
28	0.06	0.0	177°				
29	0.18	0.0	179°				
30	0.02	0.0	316°				
31	0.18	0.0	352°				
32	0.05	0.0	275°				
33	0.15	0.0	296°				
34	0.02	0.0	42°				
35	0.22	0.0	170°				
36	0.01	0.0	67°				
37	0.19	0.0	61°				
38	0.05	0.0	330°				
39	0.13	0.0	354°				
40	0.01	0.0	117°				
41	0.20	0.0	252°				
42	0.03	0.0	82°				
43	0.16	0.0	174°				
44	0.06	0.0	305°				
45	0.09	0.0	49°				
46	0.06	0.0	302°				
47	0.12	0.0	349°				
48	0.02	0.0	159°				
49	0.09	0.0	246°				
50	0.02	0.0	133°				
51	0.06	0.0	230°				
52	0.02	0.0	13°				
53	0.08	0.0	132°				
54	0.08	0.0	47°				
55	0.06	0.0	64°				
56	0.01	0.0	357°				
57	0.04	0.0	345°				
58	0.05	0.0	56°				
59	0.07	0.0	248°				
60	0.01	0.0	344°				
61	0.05	0.0	175°				
62	0.03	0.0	138°				
63	0.03	0.0	106°				

# 1/3 hp Capacitor-Run Motor

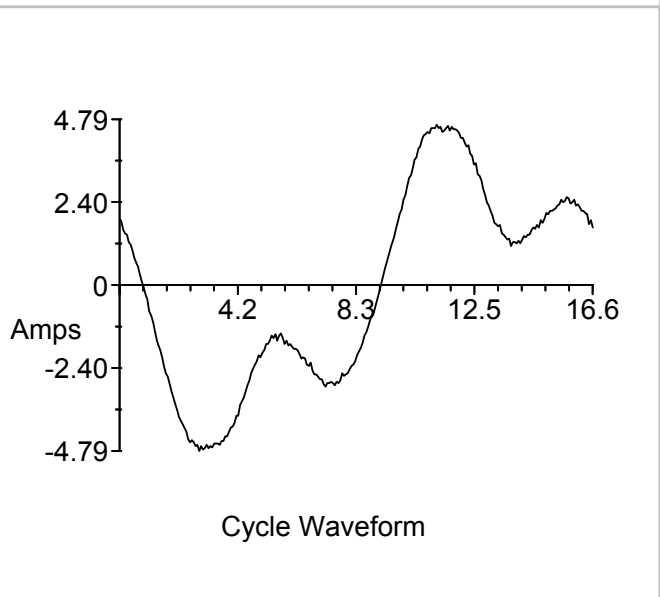


# The voltage THD is 0.7% but the current THD is 49%, almost all third!

Event: 1 Of 64  
Duration: 3 Cycles

Event Triggered by Time  
Event Trigger Cycle 1

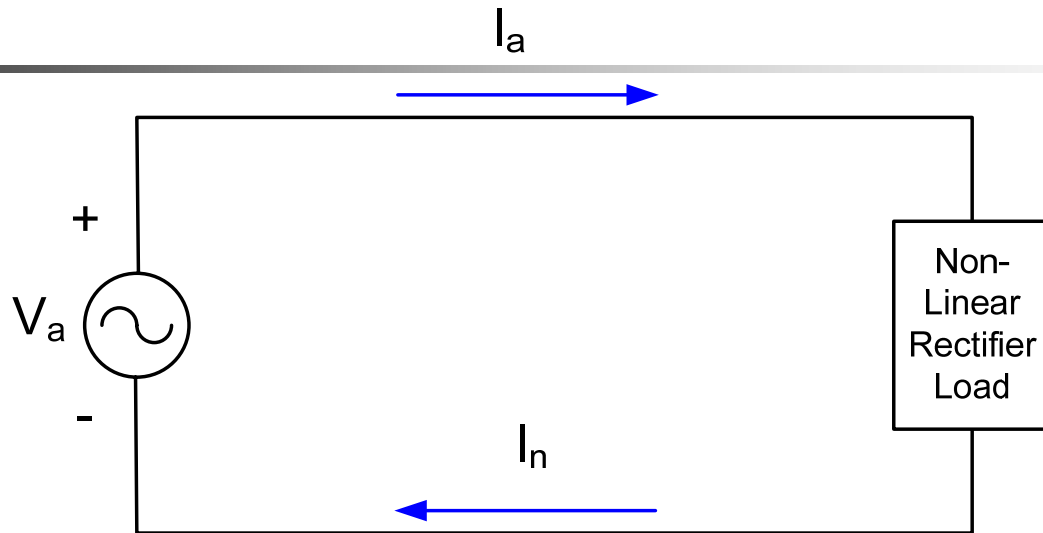
Time: 10/28/2003 18:32:36.950  
Input: Ia Amps  
Cycle: 1



Total Harmonic Distortion	49.04 %
Odd Contribution	48.96 %
Even Contribution	2.81 %
RMS Of Fundamental	2.55 A
RMS Of Fund + Harm	2.84 A
K Factor	2.93

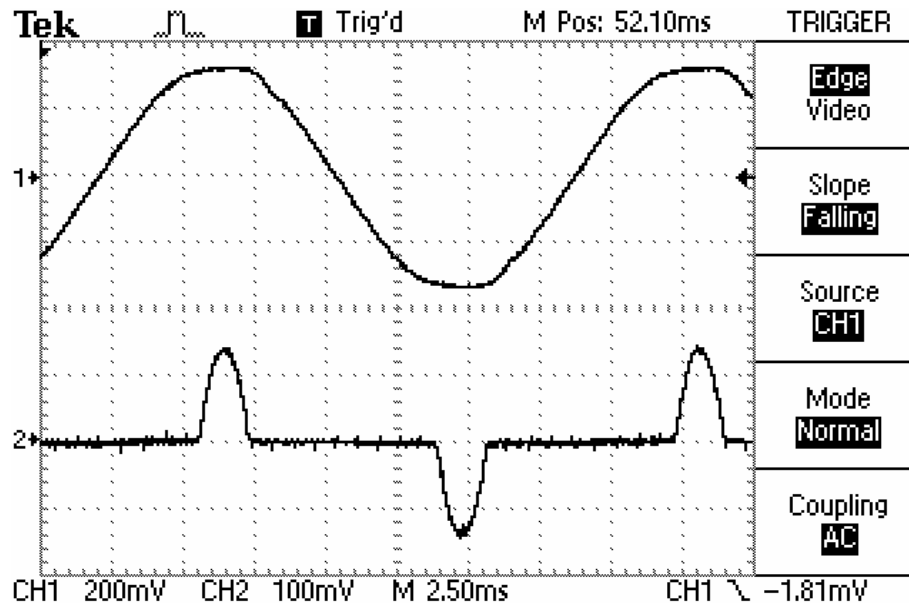
Harm Fund	% Of Fund	Amps	Angle	Harm Fund	% Of Fund	Amps	Angle
2	2.20	0.1	3°	2	2.20	0.1	3°
3	48.74	1.2	292°	4	1.02	0.0	338°
5	3.24	0.1	86°	6	0.70	0.0	32°
7	2.65	0.1	206°	8	0.31	0.0	61°
9	1.39	0.0	75°	10	0.49	0.0	31°
11	1.02	0.0	263°	12	0.29	0.0	342°
13	0.73	0.0	209°	14	0.08	0.0	88°
15	0.24	0.0	332°	16	0.45	0.0	80°
17	0.26	0.0	64°	18	0.09	0.0	102°
19	0.26	0.0	255°	20	0.27	0.0	115°
21	0.38	0.0	36°	22	0.21	0.0	85°
23	0.15	0.0	228°	24	0.10	0.0	35°
25	0.19	0.0	353°	26	0.23	0.0	59°
27	0.16	0.0	355°	28	0.13	0.0	80°
29	0.25	0.0	317°	30	0.30	0.0	197°
31	0.13	0.0	89°	32	0.15	0.0	178°
33	0.14	0.0	312°	34	0.16	0.0	332°
35	0.04	0.0	284°	36	0.19	0.0	208°
37	0.17	0.0	244°	38	0.25	0.0	242°
39	0.25	0.0	13°	40	0.05	0.0	216°
41	0.21	0.0	16°	42	0.19	0.0	1°
43	0.08	0.0	178°	44	0.09	0.0	229°
45	0.38	0.0	77°	46	0.08	0.0	209°
47	0.09	0.0	93°	48	0.28	0.0	213°
49	0.18	0.0	178°	50	0.22	0.0	285°
51	0.15	0.0	140°	52	0.08	0.0	246°
53	0.16	0.0	103°	54	0.15	0.0	318°
55	0.25	0.0	177°	56	0.26	0.0	40°
57	0.14	0.0	357°	58	0.08	0.0	330°
59	0.29	0.0	157°	60	0.37	0.0	277°
61	0.12	0.0	290°	62	0.06	0.0	261°
63	0.38	0.0	31°				

# Single-Phase PC Load



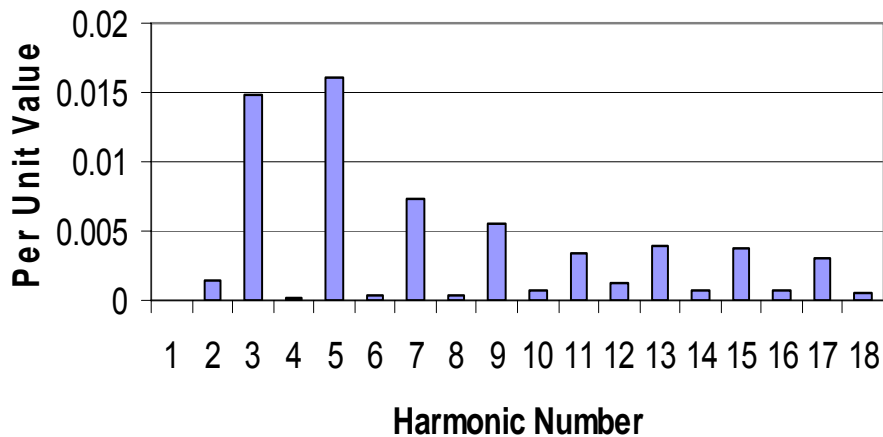
Voltage (notice the distortion near the peaks)

Phase current



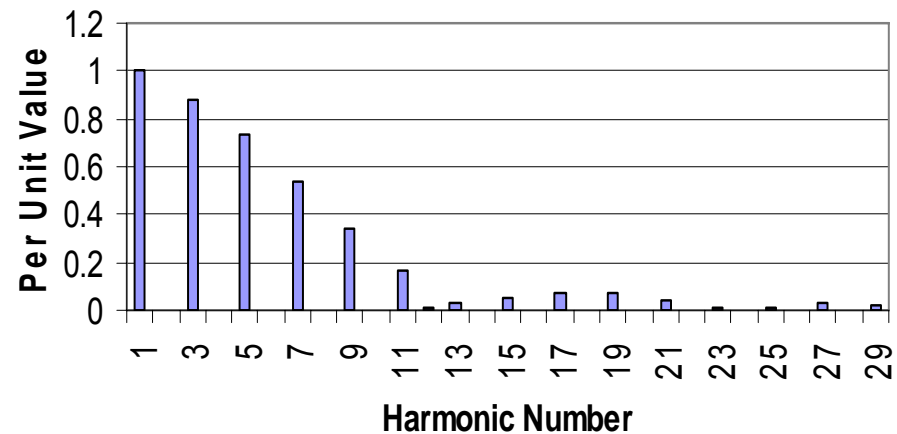
# Harmonic Analysis

## Voltage without Fundamental



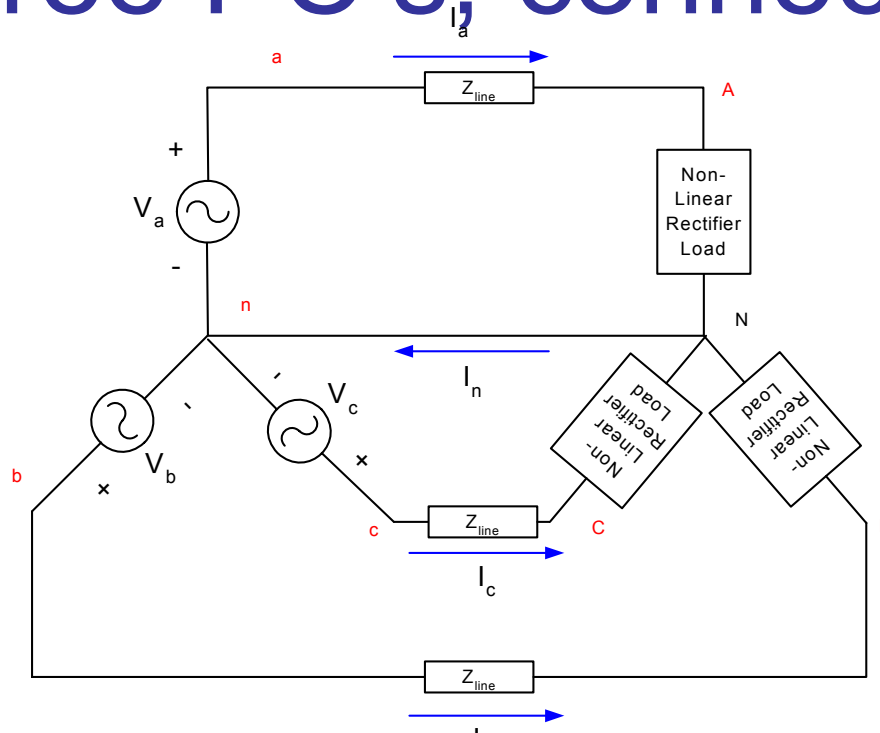
Voltage THD = 2.5%

## Phase Current Harmonics



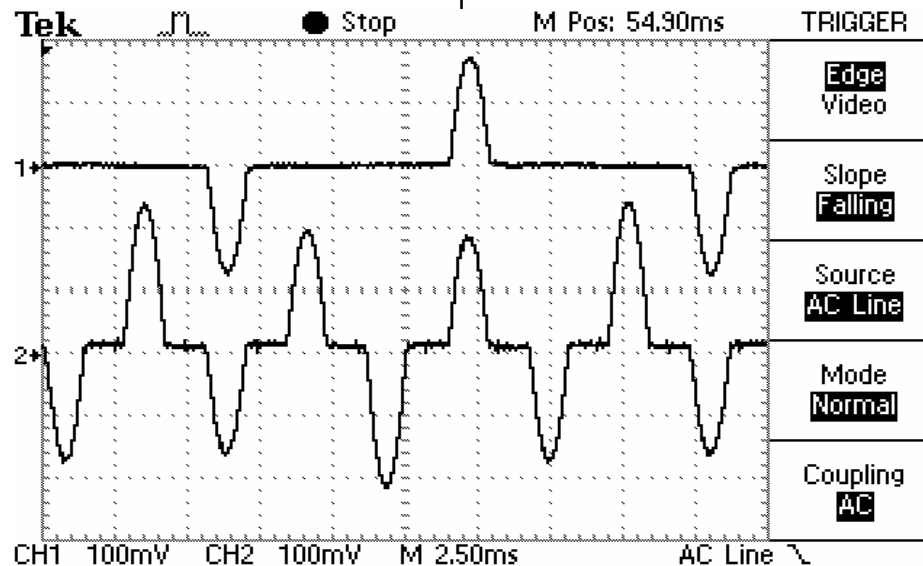
Current THD = 133%

# Three PC's, connected in Y



Phase B Current

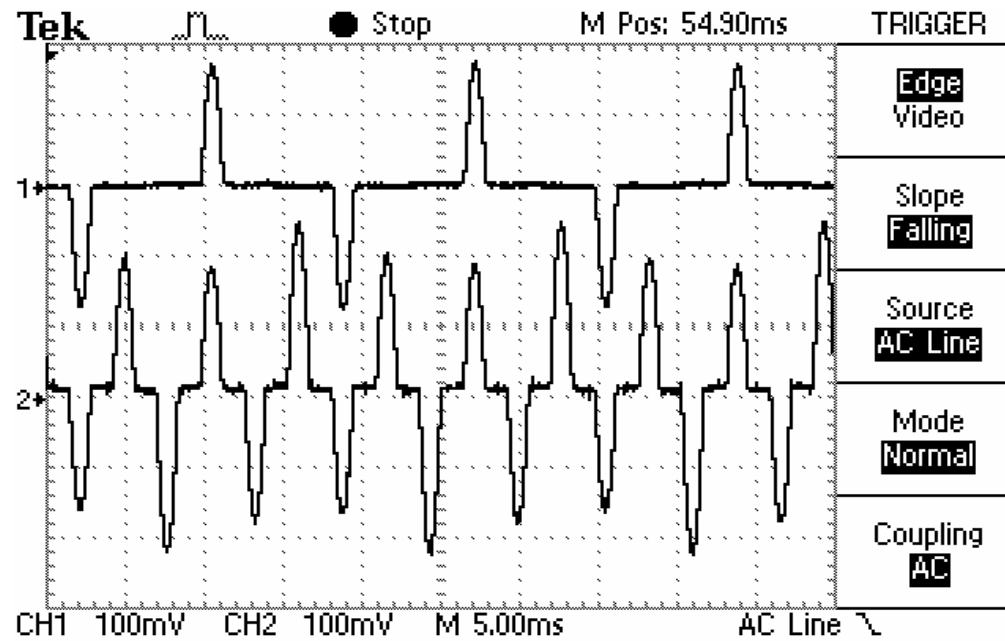
Neutral Current



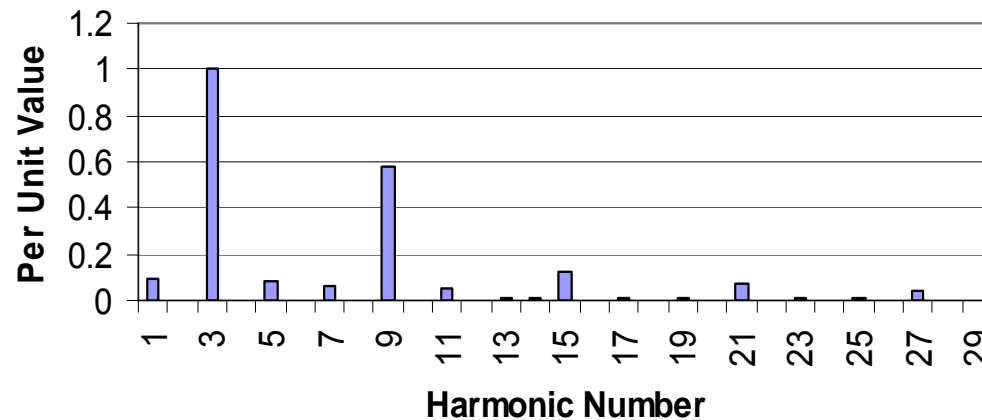
# Harmonic Analysis

Phase A

Neutral



## Neutral Current Harmonics





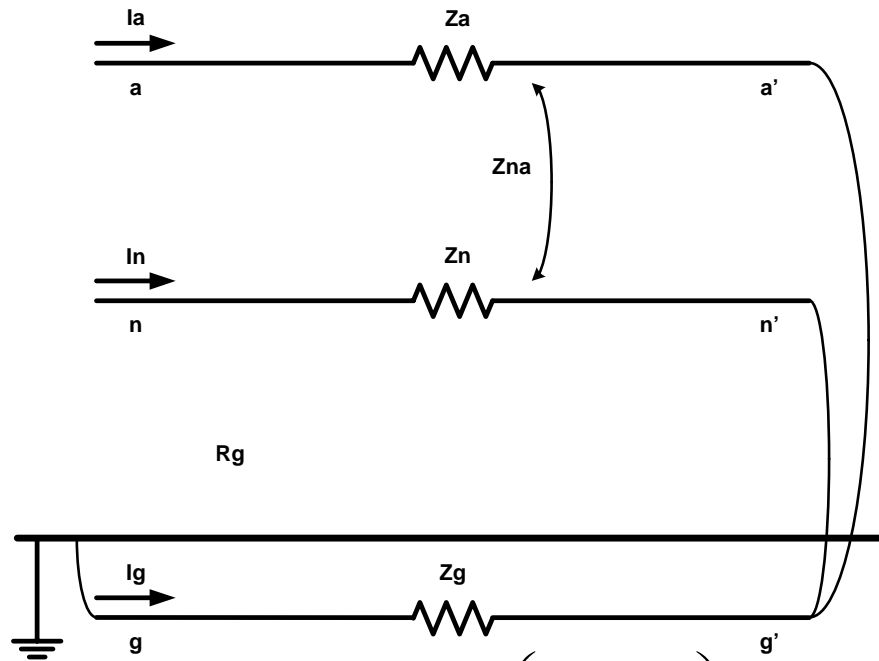
# Research Objectives

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- Develop detailed models for power system components, including nonlinear devices, tailored for NEV analysis
  - Need a 4-wire model
- Construct a multiphase harmonic load flow algorithm to obtain the NEV directly
  - The elevated NEV is due to load current, not fault current
- Analyze NEV problem in distribution systems with a large number of nonlinear devices distributed within the network
  - The focus is on simple distribution networks without parallel bonded utilities to get an understanding of the problem.



# Transmission Line Model I

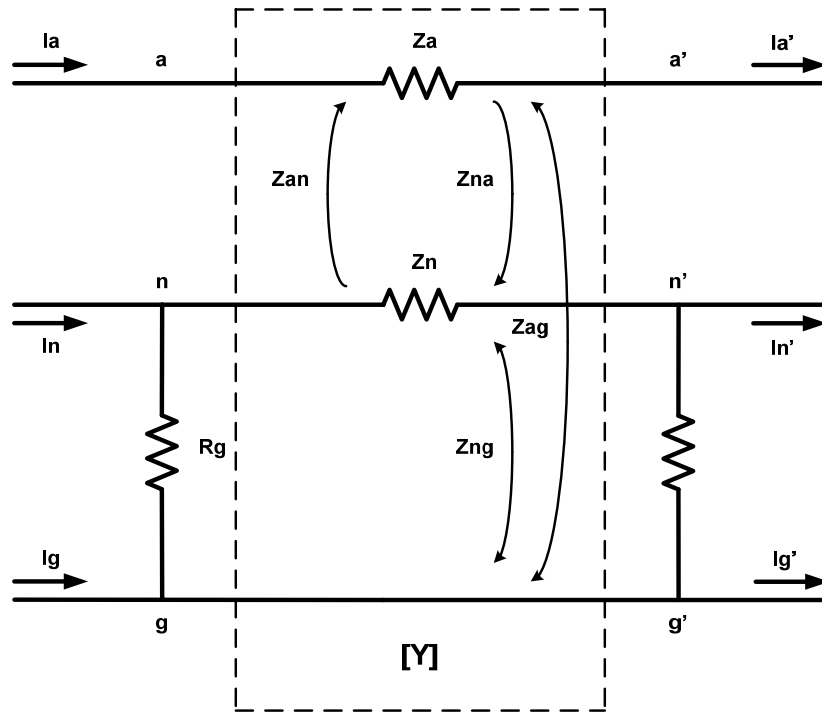


Carson's Line

$$Z_{ii-g} = R_i + j2\omega T \ln \left( \frac{S_{ii}}{GMR_i} \right) + (4\omega P + j4\omega Q)T \Omega/\text{mi}$$

$$Z_{ij-g} = j2\omega T \ln \left( \frac{S_{ij}}{d_{ij}} \right) + (4\omega P + j4\omega Q)T \Omega/\text{mi}$$

# Transmission Line Model II



Practical Distribution Line

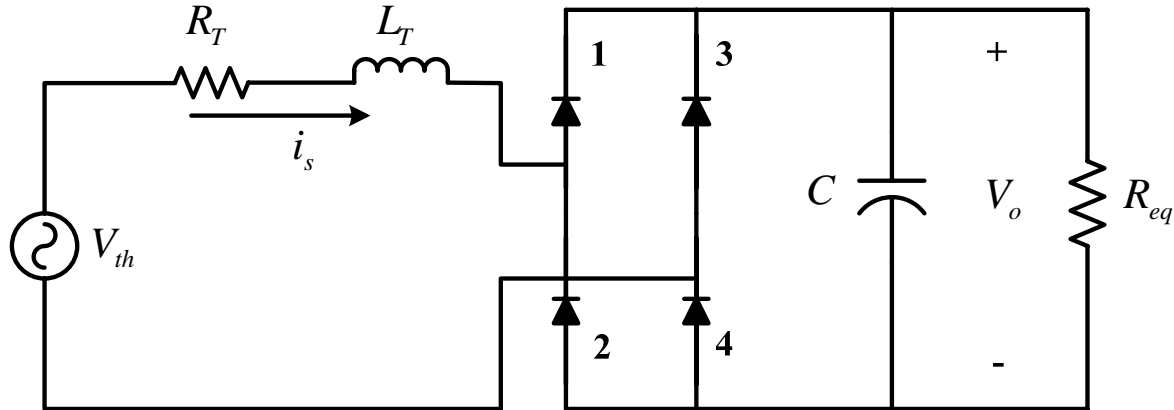
$$I_a + I_n + I_g = 0$$

$$\begin{aligned} V_{ii'} + V_{g'g} &= V_i - V_{i'} + V_{g'} - V_g \\ &= V_{ig} - V_{i'g'} \end{aligned}$$

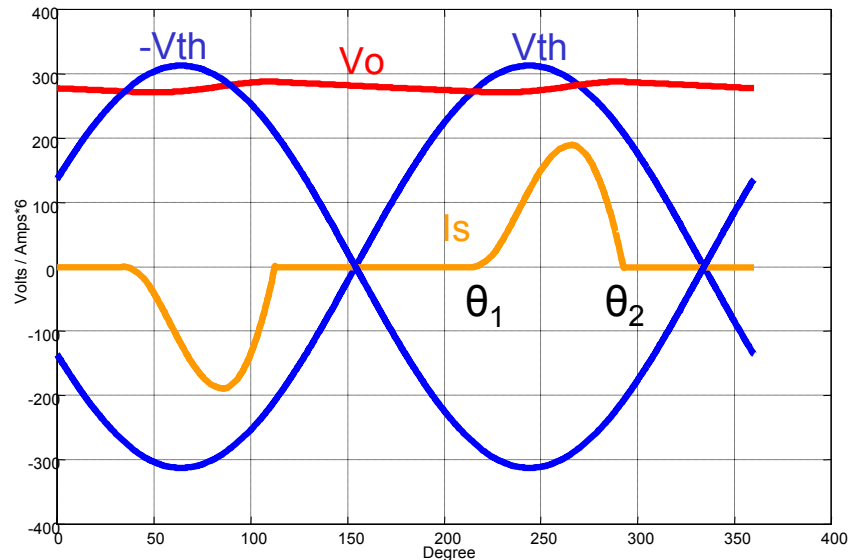
$$\begin{bmatrix} V_{ag} \\ V_{ng} \end{bmatrix} - \begin{bmatrix} V_{a'g'} \\ V_{n'g'} \end{bmatrix} = \begin{bmatrix} Z_{aa-g} & Z_{an-g} \\ Z_{an-g} & Z_{nn-g} \end{bmatrix} \begin{bmatrix} I_a \\ I_n \end{bmatrix}$$

By taking advantage of the Kirchhoff Current Law, loop voltage equations can be converted to branch voltage equations using the same loop impedances. Thus, we can solve for the phase-to-ground and neutral-to-ground voltage directly.

# Single Phase Rectifier Waveform



The input current to the rectifier is a function of the input voltage waveshape and circuit parameters. An iterative procedure is used to find  $\theta_1$  and  $\theta_2$ . These are used to determine the current spectrum.





# Multiphase Harmonic Load Flow

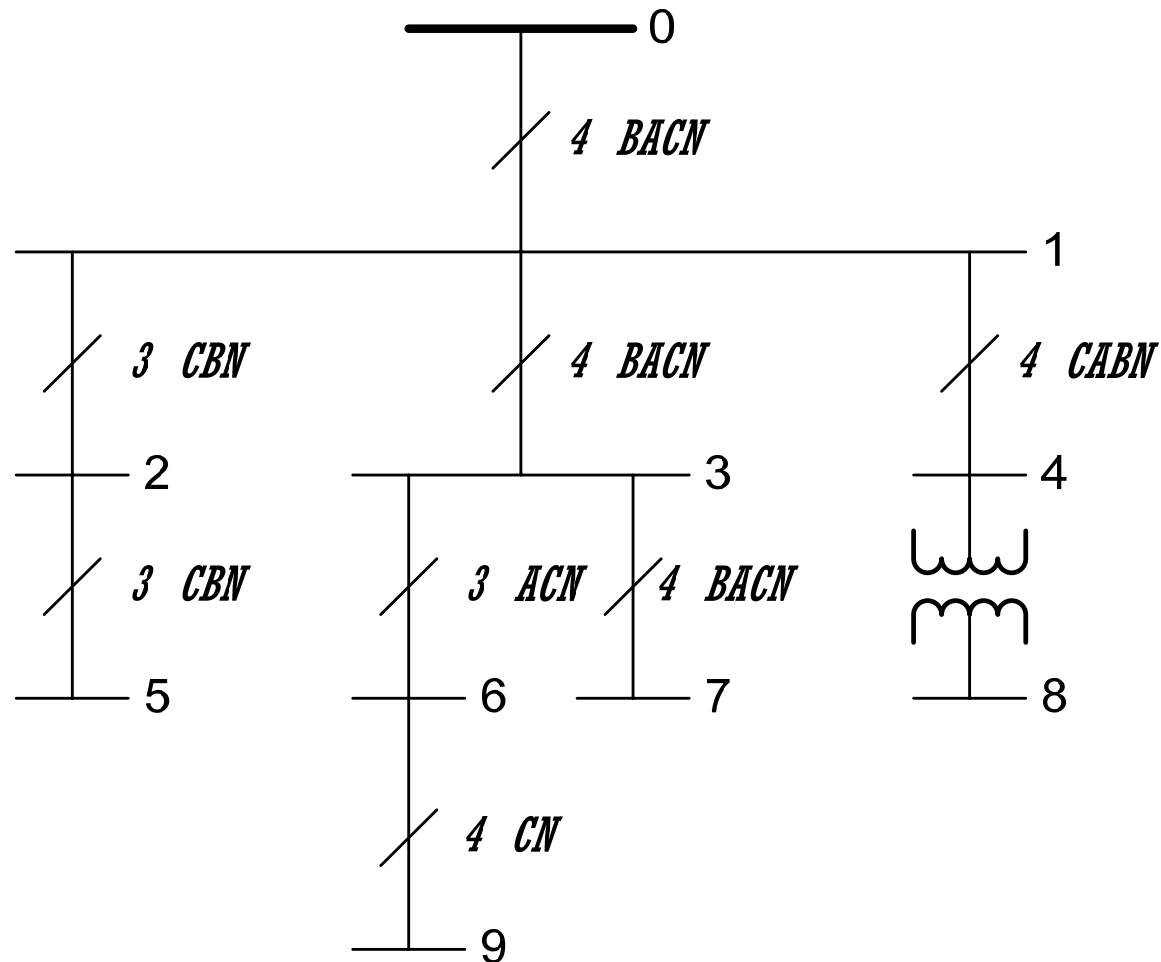
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This is used to determine the voltage spectra at all nodes, including the neutral, with respect to local earth.

- Given the node voltages from initial guess or previous iteration results, calculate the nodal current injections
- Add up all the branch currents, starting from branch farthest away from source back to the root node
- Calculate voltage drop across each branch using the branch currents, and update nodal voltage from source out to the ends of network
- Compare with previous iteration's node voltages for convergence

# Test on IEEE Example Distribution System

IEEE TEST SYSTEM





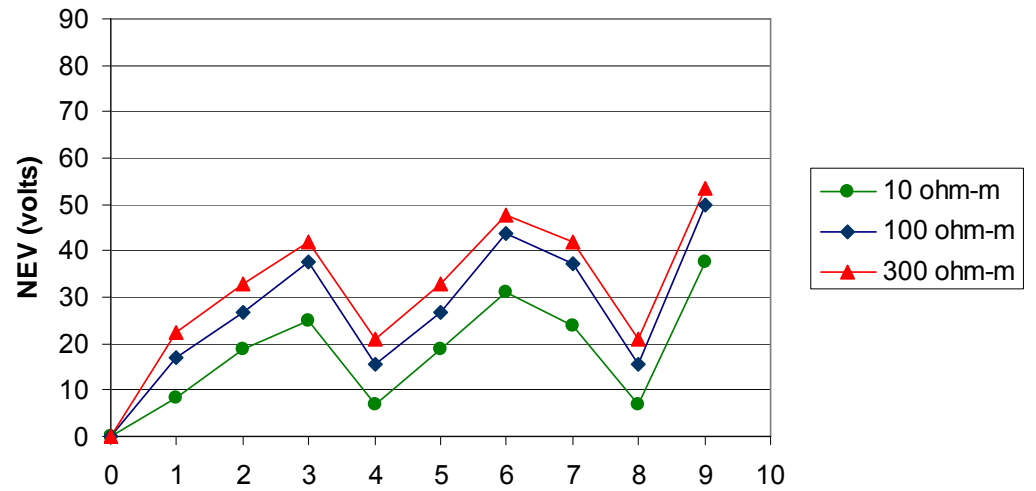
# Test Scenarios

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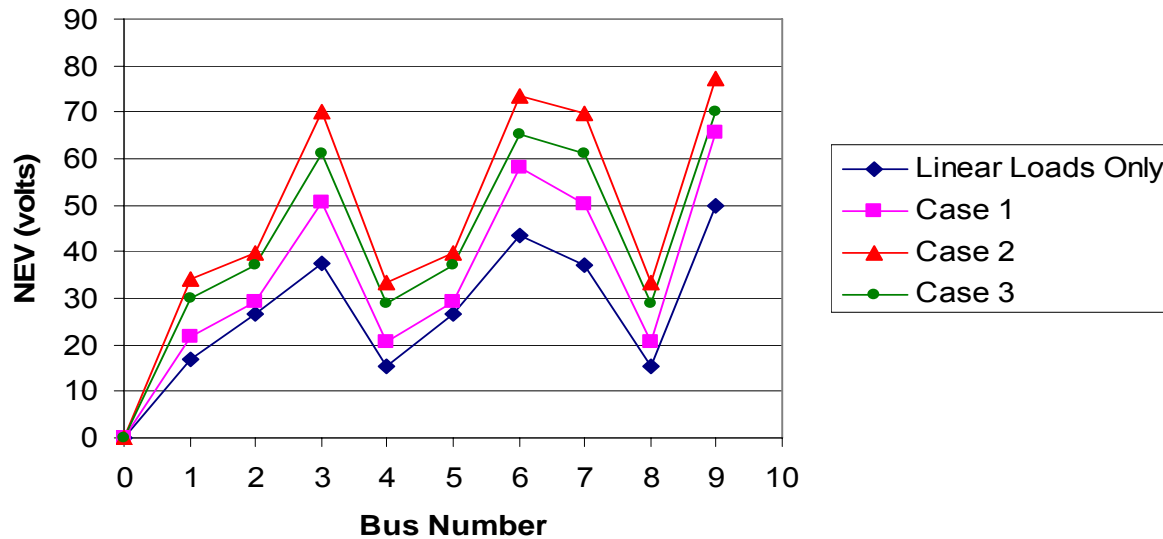
- Regular loads at different earth resistivities
  - $\rho = 10, 100, 300 \Omega\text{-m}$
- Harmonic loads with different phasing using  $\rho = 100$  (corresponds to  $R_g = 30\Omega$ )
  - Case 1: single rectifier @  $1\phi$  bus
  - Case 2: balanced rectifiers @  $3\phi$  bus
  - Case 3: unbalanced rectifiers @  $3\phi$  bus

# Test Results

## Fundamental Load Test



## Harmonic Load Test





# Conclusion

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- Triplen harmonics are present in 4-wire distribution networks, particularly those with residential loads.
- The traditional modelling techniques do not enable computation of the Neutral-to-Local Earth Voltage.
- A model has been developed which, in conjunction with a harmonic load flow, enables computation of the neutral-to-local earth voltage.
- Accurate load modeling will provide more accurate results, but the more-traditional and simple current injection models will provide reasonably accurate results.
- Future work will include longer feeders, models of other non-linear load types (e.g., motors), distributed loads, and field tests.