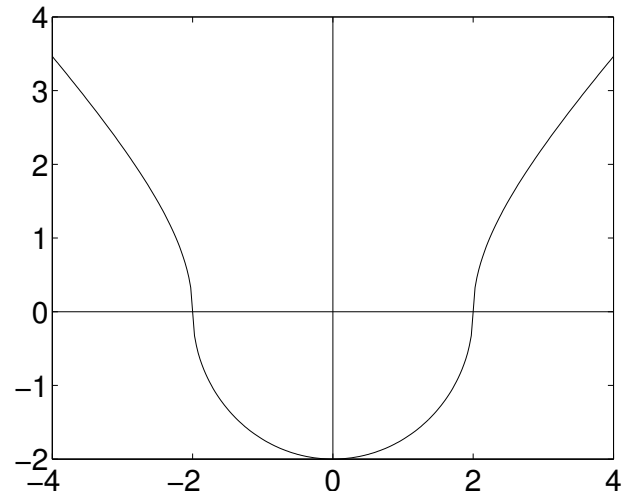


The next example shows how an expert may manipulate decorations explicitly to give a function, defined piecewise by different formulas in different regions of its domain, the best possible decoration. Suppose that

$$f(x) = \begin{cases} f_1(x) := \sqrt{x^2 - 4} & \text{if } |x| > 2, \\ f_2(x) := -\sqrt{4 - x^2} & \text{otherwise,} \end{cases}$$

see the diagram.



The function consists of three pieces, on regions $x \leq -2$, $-2 \leq x \leq 2$ and $x \geq 2$, that join continuously at region boundaries, but the standard gives no way to determine this continuity, at run time or otherwise. For instance, if f is implemented by the case function, the continuity information is lost when evaluating it on, say, $x = [1, 3]$, where both branches contribute for different values of $x \in x$.

However, a user-defined decorated interval function as defined below provides the best possible decorations.

```
function  $y_{dy} = f(x_{dx})$ 
   $u = f_1(x \cap [-\infty, -2])$ 
   $v = f_2(x \cap [-2, 2])$ 
   $w = f_1(x \cap [2, +\infty])$ 
   $y = \text{convexHull}(\text{convexHull}(u, v), w)$ 
   $dy = dx$ 
```

The user's knowledge that f is everywhere defined and continuous is expressed by the statement $dy = dx$, propagating the input decoration unchanged. f , thus defined, can safely be used within a larger decorated interval evaluation.