12.13.3. Boolean functions of intervals.

The functions listed in §10.6.3 shall be handled in the same way as those in §12.13.1.

If  $\mathbb{T}$ -version of the function isMember(m, x) is provided, the number format  $\mathbb{F}$  of the argument m should be compatible with  $\mathbb{T}$ . An implementation may provide several  $\mathbb{T}$ -versions, with different formats of m. If  $\mathbb{T}$  is a 754-conforming type, versions should be provided with the argument m of any supported 754 format of the same radix as  $\mathbb{T}$ .

12.13.4. Extended interval comparisons.

How the operations in §10.6.4 are handled at Level 2 is implementation-defined.

12.13.5. Exact reduction operations. An implementation that provides 754-conforming type for the parent format  $\mathbb{F}$  should provide an accumulator format datatype  $A(\mathbb{F})$  associated with the  $\mathbb{F}$ , and associated operations. An  $A(\mathbb{F})$  datum z is capable to represent exactly dot products of vectors of any reasonable length of arbitrary finite  $\mathbb{F}$ -numbers.

The following operations should be provided.

- convert converts from an accumulator format to a floating-point format, or vice versa, or from one accumulator format to another.
- exactAdd and exactSub adds or subtracts two accumulator or floating-point format operands, of which at least one is an accumulator, giving an accumulator format result.
- exactFma computes z + x \* y where z has an accumulator format and x, y are of floating-point format, giving an accumulator format result.
- exactDotProduct. Let a and b be vectors of length n holding floating-point numbers of format  $\mathbb{F}$ . Then exactDotProduct(a, b) computes  $a \cdot b = \sum_{k=1}^{n} a_k b_k$  exactly, giving an accumulator format result.

The result of all operations may be converted if necessary to a specified result format by application of the convert operation.

[Example. The Complete Arithmetic, specified by Kulisch and Snyder [5],[4], is an example of implementation of accumulator format and exact reduction operations. The recommended accumulator format for the binary64 format in the Complete Arithmetic has 4 bits for sign and status, 2134 bits before the point, and 2150 after the point, for a total of 4288 bits or 536 bytes; this allows for at least  $2^{88}$  multiply-adds before overflow can occur.