

11.11.1. *Bare and decorated interval literals.*

This subclause defines an **interval literal**: a (text) string that denotes a bare or decorated interval. This entails defining a **number literal**: a string, occurring within an interval literal, that denotes an extended-real number. A number literal that denotes a finite integer is an **integer literal**.

The interval denoted by an interval literal is its *value* (as an interval literal). Any other string has no value in that sense. For convenience a string is called *valid* or *invalid* (as an interval literal) according as it does or does not have such a value. The usage of value, valid and invalid for number and integer literals is similar.

[*Note. The notions of number and integer literal are only used in this subclause. Interval literals are used as input to `text2interval`, see §11.11.8. The definition of interval literal is not intended to constrain the syntax and semantics that a language might use to denote intervals in other contexts.*]

This definition of an interval literal s is placed in Level 2 because its use is not mandatory at Level 1, see §9.6.1. However the value of s is a Level 1 interval x . Within s , conversion of a number literal to its value shall be done as if in infinite precision, ignoring any default or explicit language-defined precision specification. Conversion of x to a Level 2 datum y is a separate operation. In all cases y shall contain x ; typically y is the \mathbb{T} -hull of x for some interval type \mathbb{T} .

[*Examples.*

- The interval denoted by the literal `[1.2345]` is the Level 1 single-point interval $x = [1.2345, 1.2345]$. However the result of $\mathbb{T}\text{-text2interval}("[1.2345])$, where \mathbb{T} is the 754 *infsup* binary64 type, is the interval, approximately $[1.2344999999999999, 1.2345000000000002]$, whose endpoints are the nearest binary64 numbers either side of 1.2345.
- Suppose the host language is C/C++. There, conversion of a number literal to a floating point format is considered part of its value, and a “floating-suffix” can be added to change this. E.g., `1.2345f` denotes 1.2345 rounded to the nearest float (single-precision)—instead of to the nearest double, which is the default. This is ignored within an interval literal: `1.2345` and `1.2345f` both denote the mathematical number 1.2345.

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The following forms of number literal shall be supported.

- (1) A number literal³ in the syntax provided by the host language of the implementation, in decimal or any other supported radix.
- (2) Either of the strings `inf` or `infinity`, ignoring case, optionally preceded by `+`, with value $+\infty$; or preceded by `-`, with value $-\infty$.
- (3) A string in the hexadecimal-significand form of IEEE 754-2008, §5.12.3, with the value specified there.

The following form of number literal should be supported. An implementation may restrict the support, by limiting the length of literal strings or in other ways.

- (4) A string p/q , that is p and q separated by the `/` character, where p, q are integer literals in the syntax provided by the host language of the implementation, in decimal or any other supported radix, with p optionally signed and $q > 0$. Its value is the exact rational number p/q .

[*Note. These categories need not be mutually exclusive, e.g., in C/C++, form (3) is included in (1).*]

Unit in last place. The “uncertain form” of interval literal, below, uses the notion of the *unit in the last place* of a number literal s of some radix b , possibly containing a point but without an exponent. Thus ignoring any radix-specifying code (such as C’s initial `0x` for hexadecimal), s is a nonempty string each of whose characters is a radix- b digit or a point “.”, and which contains at least one digit and at most one point. Its *last place* is the integer $p \leq 0$ defined as follows. If s contains no point then $p = 0$. Otherwise $p = -n$ where n is the number of digits after the point. Then $\text{ulp}(s)$ is defined to equal b^p . When context makes clear, “ x ulps of s ” or just “ x ulps”, is used to mean $x \times \text{ulp}(s)$. [*Example. For the decimal strings 123 and 123. , as well as 0 and 0. , the last place is 0 and one ulp is 1. For .123 and 0.123 , as well as .000 and 0.000 , the last place is -3 and one ulp is 0.001.*]

³“floating constant” in C, “real literal constant” in Fortran, “real numeric literal” in Ada, etc.

Bare intervals. The forms of bare interval literal that shall be supported are listed below. To simplify stating the needed constraints, e.g. $l \leq u$, the number literals l, u, m, r are identified with their values. Space shown between elements of a literal, below, denotes zero or more characters that count as whitespace in the host language. [Note. Some characters, e.g., newline, might be whitespace in some contexts but not others.]

Constants: The string [empty], ignoring case, whose value is the empty set \emptyset ; and the string [entire], ignoring case, whose value is the whole line \mathbb{R} .

Inf-sup form: A string $[l, u]$ where l and u are number literals with $l \leq u$, $l < +\infty$ and $u > -\infty$, see §9.2. Its value is the mathematical interval $[l, u]$. A string $[x]$ is equivalent to $[x, x]$.

Uncertain form: a string $m ? r u E$ where: m is a decimal number literal of form (1) above, without exponent; r is empty or is a non-negative decimal integer literal *ulp-count*; u is empty or is a *direction character*, either **u** (up) or **d** (down); and E is empty or is an *exponent field* comprising the character **e** followed by an optionally signed decimal integer literal *exponent* e . No whitespace is permitted within the string.

With **ulp** meaning $\text{ulp}(m)$, the literal $m?$ by itself denotes m with a symmetrical uncertainty of half an ulp, that is the interval $[m - \frac{1}{2}\text{ulp}, m + \frac{1}{2}\text{ulp}]$. The literal $m?r$ denotes m with a symmetrical uncertainty of r ulps, that is $[m - r \times \text{ulp}, m + r \times \text{ulp}]$. Adding **d** (down) or **u** (up) converts this to uncertainty in one direction only, e.g. $m?d$ denotes $[m - \frac{1}{2}\text{ulp}, m]$ and $m?ru$ denotes $[m, m + r \times \text{ulp}]$. Finally the exponent field if present multiplies the whole interval by 10^e , e.g. $m?ruee$ denotes $10^e \times [m, m + r \times \text{ulp}]$.

[Examples. Assuming the common types of decimal number literals are provided:

Form	Literal	Exact value
Inf-sup	[1.e-3, 1.1e-3]	[0.001, 0.0011]
	[-Inf, 2/3]	$[-\infty, 2/3]$
Uncertain	30?	[29.5, 30.5]
	3.56?	[3.555, 3.565]
	3.56?1	[3.55, 3.57]
	3.56?1e2	[355, 357]
	3.560?2	[3.558, 3.562]
	3.560?2u	[3.560, 3.562]

]

A formal description of bare interval literals is by the following grammar (using the notation of 754§5.12.3) which defines a `bareIntvlLiteral`, subject to the constraints on l, u, m, r, p, q stated above. `anycase(s)` matches all upper/lower case variants of the string s , e.g. `anycase("ab")` matches any of "ab", "Ab", "aB", "AB".

⚠ Meta-characters are temporarily colored red, to help spot any meta-syntax-errors in this grammar.

```

sign          [+-]
digit         [0123456789]
natural       {digit} +
langNumLit    {number literal of host language}
langNumLitMant {mantissa of number literal of host language}
langNumLitExp "e" {exponent of number literal of host language}
sp            {whitespace character of host language} *
infLit        {sign} ? ( anycase("inf") | anycase("infinity") )
hexNumLit     {see 754§5.12.3}
ratNumLit     {sign} ? {digit} + "/" {digit} +
numberLiteral ( {langNumLit} | {infLit} | {hexNumLit} | {ratNumLit} | )
pointIntvl    "[" {sp} {numberLiteral} {sp} "]"
infSupIntvl   "[" {sp} {numberLiteral} {sp} "," {sp} {numberLiteral} {sp} "]"
uncertIntvl   {langNumLitMant} "??" {natural} ? [du]? {langNumLitExp} ?
constIntvl    ( anycase("[empty]") | anycase("[entire]") )
bareIntvlLiteral ( {pointIntvl} | {infSupIntvl} | {uncertIntvl} | {constIntvl} )

```

Decorated intervals. The syntax of decorated interval literals is given by extending the above grammar as follows, to define a `decoratedIntvlLiteral`.

```

connectChar      {language-defined character}
decorationLit    ( "ill" | "trv" | "def" | "dac" | "com" )
decoratedIntvlLiteral {bareIntvlLiteral} {connectChar} {decorationLit}

```

That is, s is a bare interval literal $s\mathbf{x}$, followed by a language-defined single character c followed by a 3-character decoration string $s\mathbf{d}$. It is recommended that c be the underscore ‘_’, which is assumed here. The string $s\mathbf{d}$ is one of `ill`, `emp`, `trv`, `def`, `dac` or `com` representing the corresponding decoration dx . If $s\mathbf{x}$ has the value x , and if x_{dx} is a permitted combination according to §10.4, then s has the value x_{dx} . Otherwise s has no value as a decorated interval literal.

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