

Figure 1: Complementary Partial Orders

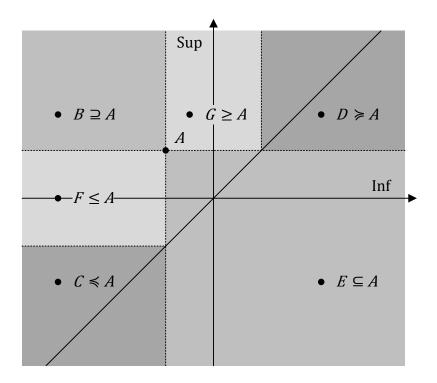


Figure 2: Family of Comparison Relations

Elementary Relation	Description	IEEE 1788 (proposed)
A = B	"A equals B"	a1 = b1 and a2 = b2
$A \subseteq B$	"A is a subset of B"	$a1 \ge b1$ and $a2 \le b2$
$A \le B$	"A is less or equal to B"	$a1 \le b1$ and $a2 \le b2$
A ≼ B	"A precedes or is equal to B"	a2 ≤ b1
$A \subset B$	"A is interior to B"	a1 > b1 and a2 < b2
A < B	"A is strictly less than B"	a1 < b1 and a2 < b2
$A \prec B$	"A precedes B"	a2 < b1

Table 1: Elementary Relations (proposed)

Relation	Fortran 95	Elementary Relations
isDisjoint(A,B)	b2 < a1 or a2 < b1	$A \prec B \text{ or } B \prec A$
isInterior(A,B)	b1 < a1 and a2 < b1	$A \subset B$
isProperSubset(A,B)	$b1 \le a1$ and $a2 < b2$ or $b1 < a1$ and $a2 \le b2$	$A \subseteq B$ and not $(A = B)$
isSubset(A,B)	b1 ≤ a1 and a2 ≤ b2	$A \subseteq B$
setIsLess(A,B)	a1 < b1 and a2 < b2	A < B
setIsLessOrEqual(A,B)	a1 ≤ b1 and a2 ≤ b2	$A \le B$
setIsEqual(A,B)	a1 = b1 and a2 = b2	A = B
certainlyIsLess(A,B)	a2 < b1	A ≺ B
certainlyIsLessOrEqual(A,B)	a2 ≤ b1	A ≼ B
certainlyIsEqual(A,B)	b2 ≤ a1 and a2 ≤ b1	$A \leq B$ and $B \leq A$
possiblyIsLess(A,B)	a1 < b2	not (B ≤ A)
possiblyIsLessOrEqual(A,B)	a1 ≤ b2	not (B ≺ A)
possiblyIsEqual(A,B)	a1 ≤ b2 and b1 ≤ a2	not (A < B or B < A)

Table 2: Fortran 95 Relations as Elementary Relations