#### LONG-REACH

#### MODIFIED mN/mN+1 ENCODING

#### CAPABLE TO PROCESS ON COUPLES OF CONTROL

#### I. FOUNDATION

The encoding method described further in this memo is based on the 8N/8N+1 encoding introduced (invented?) by William Lo during the time of IEEE P802.3bp task force [1, 2], with the following modifications.

[1] https://www.ieee802.org/3/bp/public/mar14/Lo\_3bp\_02\_0314.pdf

(1000BASE-T1 PHY Encoder Proposal For Gigabit MAC Compatibility, March 2014)

[2] https://www.ieee802.org/3/bp/public/may14/Lo\_3bp\_01\_0514.pdf

(Correction to 1000BASE-T1 PHY 8N/8N+1 Encoder Equations, May 2014)

First, it treats on the input left to right, instead of right to left as in [1, 2], to decrease the transmit (encoding) delay, namely the argument accumulation delay.

	ORIG. mN/mN+1 ENC.			MOD. mN/mN+1 ENC.	
BIT FOUND LAST BUT SENT FIRST	<del></del>	BIT FOUND FIRST BUT SENT LAST	BIT FOUND FIRST AND SENT FIRST		BIT FOUND LAST AND SENT LAST
	INPUT ORDER			INPUT ORDER	

Second, it constructs the output in a tabular manner, with functionally natural rows of bits, instead in a bit stream manner as in [1, 2], that simplifies its description and reception.

ORIG. mN/mN+1 ENC.	MOD. mN/mN+1 ENC.

Third, it provides extra signaling options, obvious with its row-based definition but hardly seen with a bit stream-based definition as in [1, 2], in the form of forced output samples.

At the same time, like [1, 2], it treats on an input stream of independent transfer units, in singles if data, that is again like in [1, 2], but in couples if control, that is new to [1, 2].

For more information on formalization and generalization of the encoding approach which lies at the heart of the described method, see the author's draft [3].

[3] https://arxiv.org/pdf/2302.13589, pp. 25-36

## II. PRINCIPLES OF OPERATION — ENCODING PATTERNS, N=4

In the tables below, encoding input patterns for a span of N = 4 transfer units are listed. To fit into the output capacity, some patterns have aliases, therefore the output of such patterns can be unambiguously decoded only with the knowledge of its adjacent outputs, previous or next, in the stream. Here and further C and c mean the same (control).

### TRANSFER SPAN PATTERNS

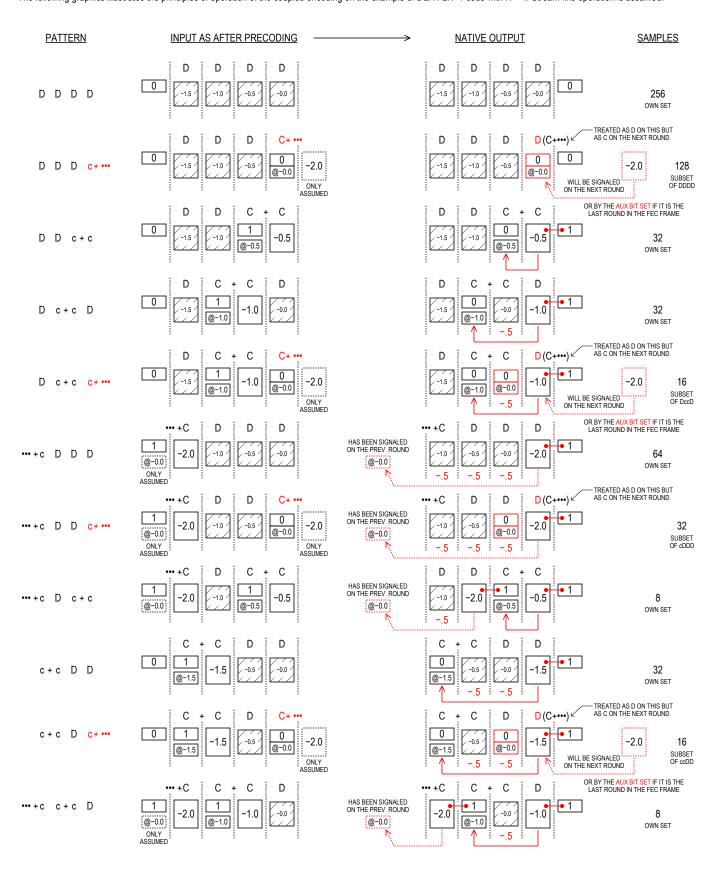
_	Р	PAT	ER	N		AS:	SUN	1ED	AS		INVA	RIANT	STRICT EVEN	S	TRICT O	DD	MD	XED
(0)	D	D	D	D		D	D	D	D	[	D D	D D						
(1)	D	D	D	С		D	D	D	C+ •••					D	D D	C+ •••		
(2)	D	D	С	D					MUST	BE TR	EATE	ED AS DDcc C	R DccD DEPENDING ON 1	THE CURRE	NT EVE	N/ODD OF	RDER	
(3)	D	D	С	С		D	D	c -	+ C				D D c+c	_				
(4)	D	С	D	D					MUST	BE TR	EATE	ED AS DccD C	R ccDD DEPENDING ON 1	THE CURRE	NT EVE	N/ODD OF	RDER	
(5)	D	С	D	С					MAY BE TE	REATE	D AS	cccc OR Dccc	OR ccDc DEPENDING ON	I THE CURF	RENT EN	ICODING (	CONTEXT	
(6)	D	С	С	D		D	C +	+ C	D					D	c + c	D		
(7)	D	С	С	С		D	C +	+ C	C+ •••					D	c + c	C+ •••		
(8)	С	D	D	D	••• +	С	D	D	D					••• + C	D D	D		
(9)	С	D	D	С	••• +	С	D	D	C+ •••					••• + C	D D	C+ •••		
(10)	С	D	С	D					MAY BE TE	REATE	D AS	cccc OR cccD	OR cDcc DEPENDING ON	I THE CURF	RENT EN	ICODING (	CONTEXT	
(11)	С	D	С	С	••• +	С	D	c -	+ C							_	••• + c D	C + C
(12)	С	С	D	D		c +	- с	D	D				c+c D D	-				
(13)	С	С	D	С		С+	- с	D	C+ •••							_	c + c	D c+•
(14)	С	С	С	D	••• +	С	C +	+ C	D					••• + C	c + c	D		
(15e)	С	С	С	c <	$\rightarrow$	С+	- с	c -	+ C				c + c	_				
(150)					<i>\_</i> +	С	C +	+ C	C+ •••					••• + C	c + c	C+ •••		
-	1	6 T	ATC	L		11	+ 1	e +	10		1 OU	Γ OF 16	3 OUT OF 16	7	OUT OF	16	2 OUT	OF 16

# TREATABLE PATTERNS

F	PATTERN		N	TREATED AS			ITS ALIAS			BECAUSE	TF	AS			
D	D	D	D	D D D	<b>←</b>	(1)	D	D	D	С		D	D	D	D(c+•••)
D	D	С	С	D D c+c											
D	С	С	D	D c+c D	<b>←</b>	(7)	D	С	С	С		D	c -	+ C	D(c+•••)
С	D	D	D	••• +c D D D	<b>←</b>	(9)	С	D	D	С	••	• + C	D	D	D(c+•••)
С	D	С	С	••• + c D c + c											
С	С	D	D	c+c D D	<b>←</b>	(13)	С	С	D	С		С	+ C	D	D(c+•••)
С	С	С	D	••• + c	<b>←</b>	(150)	С	С	С	С	••	• + C	c -	+ C	D(c+•••)
С	С	С	С	c + c											
(7 + 1e =) 8 OUT OF 17 (= 15 + 2)				•		(4	+ 10	=) 5	OUT OF	17 (=	15 +	- 2)			
	D D c c	D D D C C D C C C C	D D D D C D C C C D C C D C C C C	D D D D D C C D C D D C D D D C D C C C C D D C C C C	D D D D D D D D D D D D D D D D D D D	D D D D D       D D D D D         D D c c       D D c + c         D c c D D c + c D       →         c D D D+c D D       →         c D c c+c D c + c       ←         c c D D+c D D       ←         c c c D D+c C D       ←         c c c c D+c C + c D       ←	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	D D D D D       D D D D D       ← ← ← ← ← ← ← ← ← ← ← ← ← ← ← ← ← ← ←	D D D D D       D D D D D         D D c c       D D c + c         D c c D D C + c D       ← ← ← ← ← ← ← ← ← ← ← ← ← ← ← ← ← ← ←	D D D D D       →       (1)       D D D D         D D c c       D D c + c          D c c D D D c + c D       →       (7)       D c c         c D D D m + c D D D       →       (9)       c D D         c D c c m + c D c + c        (13)       c c D         c c c D D m + c c + c D       →       (150)       c c c         c c c c c c c c c c c c c c c c c c c	D D D D D       D D D D D         D D c c       D D c + c         D c c D D c + c D       (7) D c c c c         c D D D 0       (9) c D D c         c D c c m+c D c + c       (13) c c D c c         c c c D D m+c c + c D (150) c c c c c       (150) c c c c c	D D D D D       →       (1)       D D D C         D D c c       D D c + c       →       (7)       D c c c         D c c D D D       →       (9)       c D D c       →         c D c c       →       (1)       D D D D c       →         c D D D c c c c       →       (9)       c D D c       →         c D c c c c c c c c c c c c c c c c c c	D D D D D       D D D D D       →       (1) D D D C       D         D D C C D D C + C       D C C C D D C C C D       →       (7) D C C C D D C C C D D C C C C D D C C C C D D C C C C D D C C C C C D D C	D D D D D D D D D D D D D D D D D D D	D D D D D D D D D D D D D D D D D D D

#### II. PRINCIPLES OF OPERATION — EXAMPLE COUPLED ENCODING, 8B/9B, UT=2BT, PART 1 OF 2

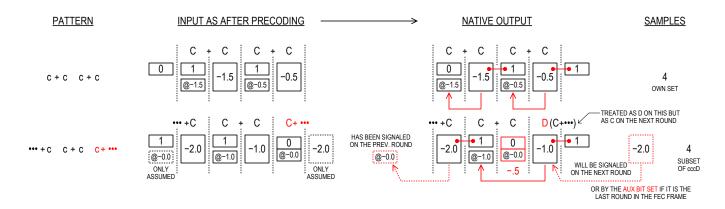
The following graphics illustrates the principles of operation of the coupled encoding on the example of a 2N / 2N+1 code with N = 4. Stream-like operation is assumed.



# Modified mN/mN+1 Encoding for P802.3dg Single Pair Ethernet (LONG-REACH CASE)

#### II. PRINCIPLES OF OPERATION — EXAMPLE COUPLED ENCODING, 8B/9B, UT=2BT, PART 2 OF 2

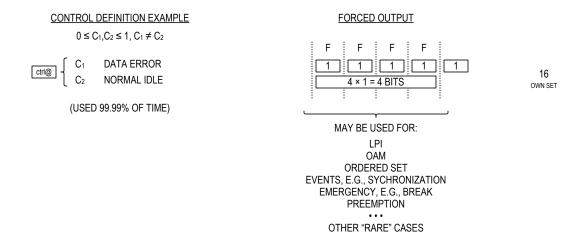
(Continued graphics from the previous page.)



#### **LEGEND**

- 0 BIT OF CONSTANT VALUE 0
- 1 BIT OF CONSTANT VALUE 1
- TWO BITS OF VARIABLE (PAYLOAD) DATA VALUE AT INPUT OFFSET -#.#, A CHOICE 1-0F-4
- @-## ONE BIT OF VARIABLE (PAYLOAD) CONTROL VALUE AT INPUT COUPLE (OFFSET, OFFSET+.5), A CHOICE 1-OF-2
- -#.# TWO BITS OF CONTROL VALUE OFFSET, A CHOICE 1-OF-4, WITH -2.0 CODED SO ITS UPPER BIT IS 0 (E.G., 2b'00), AND -0.0 NOT PRESENT
- -## OFFSET ASSUMED FROM THE LATEST TRANSFER UNIT OF THE CURRENT INPUT, EXPRESSED IN HALVES OF COUPLE PERIODS
- -.5 EXTRA DISPLACEMENT STRESSED DUE TO ENCODING
- 0 @-0.0

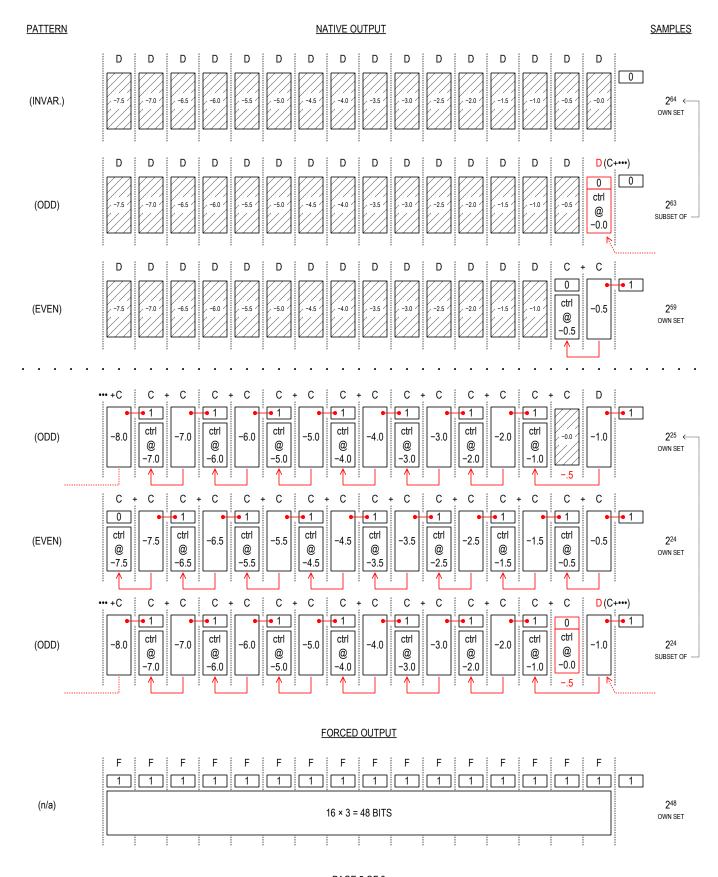
  TWO BITS TREATED AS DATA ON THE CURRENT ENCODING ROUND, BUT AS OF CONTROL ON THE NEXT.
- DECODING PATH ELEMENTS (ARROWS) AND TIPS (LINKS)



Because the most observed extra displacement is .5, the argument accumulation delay (TX\_ADD) is just twice the transfer unit time (UT), or equivalently four bit times (BT) here.

#### III. LONG-REACH COUPLED ENCODING, 64B/65B, UT=4BT — GENERAL DEFINITION

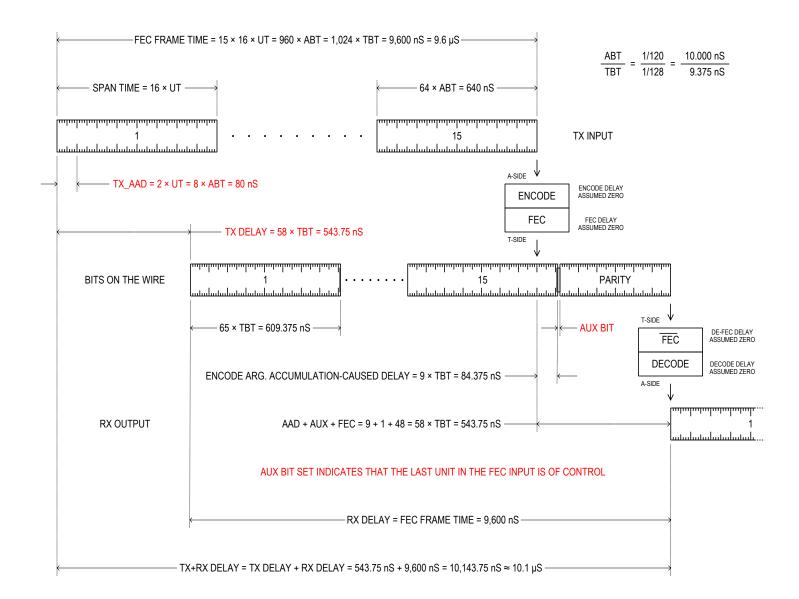
Below, all the cases of transfer units involved in the encoding are shown. A couple of two transfer units is capable to reflect 8 control symbols located with a single unit precision.



#### III. LONG-REACH COUPLED ENCODING, 64B/65B, UT=4BT — IDEAL-CASE CODING DELAYS

In a systematic FEC-based application, the ideal decoding delay is not a managed property because the respective FEC frame is decoded at once and as a whole. Therefore, the only managed property that we can optimize (minimize) here is the argument accumulation delay of the encoder at the transmitting side. At the same time, such optimization may affect back on the decoding delay: in our case, we almost neutralizes such by using the auxiliary bit to indicate on the pattern of the last encoding round in the FEC frame.

#### **CODING DELAYS**



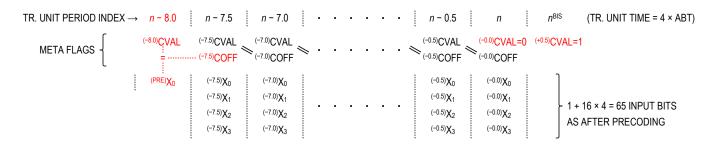
NOTE — ALL SHOWN DELAYS ARE CONSTANT AND FRAME CONTENT-INDEPENDENT.

NOTE — TRANSFER UNIT TIME (UT) = NIBBLE TIME = FOUR BIT TIMES = 4 × ABT = 40 nS.

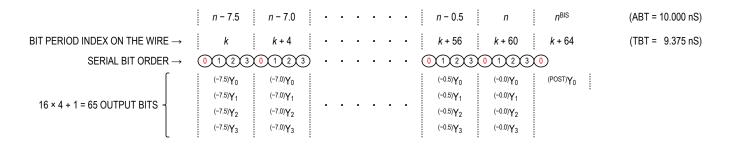
# Modified mN/mN+1 Encoding for P802.3dg Single Pair Ethernet (LONG-REACH CASE)

III. LONG-REACH COUPLED ENCODING, 64B/65B, UT=4BT — FORMAL DEFINITION, PART 1 OF 2

#### <u>INPUT</u>



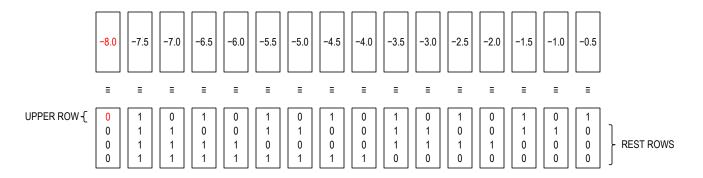
#### **OUTPUT**



### **CONSTRAINTS**

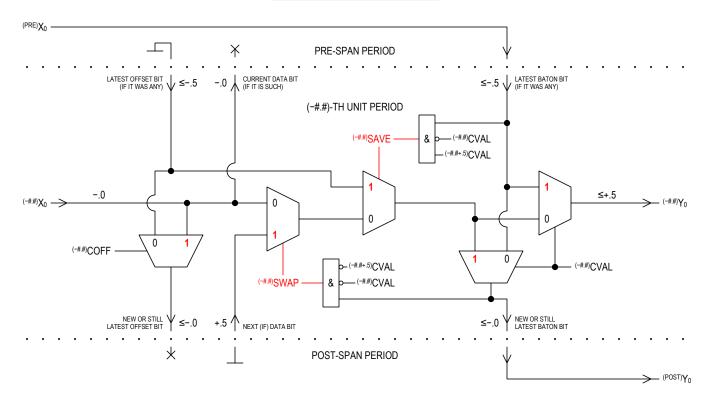
(-0.0)CVAL = 0 AND (-0.5)CVAL = 1 BY DEFINITION,  $n^{\rm BIS}$  IS AN IMAGINARY PERIOD (-#.#)CVAL := 1 IF THE (-#.#)-TH UNIT PERIOD IS OF CONTROL VALUE, OTHERWISE 0 (-#.#)COFF := 1 IF THE (-#.#)-TH UNIT PERIOD IS OF CONTROL OFFSET, OTHERWISE 0 (-#.#)COFF = (-#.5)CVAL AND (PRE)X<sub>0</sub> = (-7.5)COFF = (-8.0)CVAL BY DEFINITION (-#.#)X<sub>0</sub> OF THE OFFSET CODE INDICATING ON THE (-8.0)-TH PERIOD MUST BE 0 AUX := 1 IF THE LAST ROUND IN THE FEC FRAME IS OF ....C+•••, OTHERWISE 0

#### OFFSET CODES (RECOMMENDED)

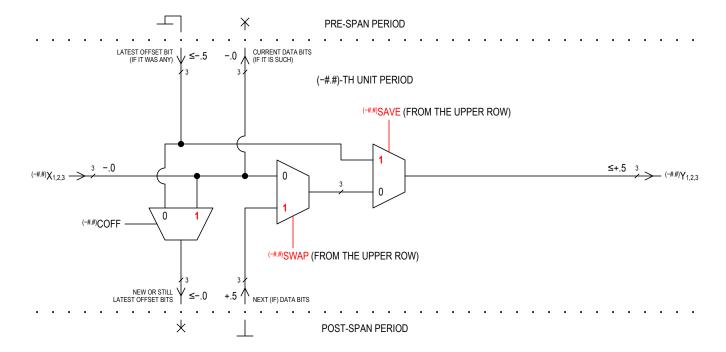


III. LONG-REACH COUPLED ENCODING, 64B/65B, UT=4BT — FORMAL DEFINITION, PART 2 OF 2

#### RELAYING OF BITS IN THE UPPER ROW



#### RELAYING OF BITS IN THE REST ROWS



# Modified mN/mN+1 Encoding for P802.3dg Single Pair Ethernet (LONG-REACH CASE)

### III. LONG-REACH COUPLED ENCODING, 64B/65B, UT=4BT — PRECODER OPERATION (INFORMATIVE)

As shown below, the precoder works like a pipeline and treats on every MII input cycle to form the input bits, X's, and meta flags, CVAL and COFF, to the coupled encoder at the respective transfer unit period, n. Because the result depends on the preceding, current, and following MII input cycles only, combining the precoder and encoder into an integral function does not lengthen the argument accumulation delay over that of the encoder itself, i.e., two transfer unit times.

#### PER-UNIT PRECODING FUNCTION

