

## Summary

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Differences exist between documents.

### New Document:

[han\\_3ca\\_2a\\_0118](#)

3 pages (137 KB)

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Used to display results.

### Old Document:

[han\\_3ca\\_2\\_0118](#)

3 pages (136 KB)

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[Get started: first change is on page 2.](#)

No pages were deleted

## How to read this report

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 indicates pages were moved.

# DRAFT

## Low Density Parity Check Coding

The bit sequence input for a given code block to channel coding is denoted by  $u_1 \ u_2 \ \dots \ u_K$ , where  $K$  is the number of bits to be encoded. The parity check bit sequence produced by FEC Encoder is denoted by  $p_1 \ p_2 \ \dots \ p_M$ , where  $M$  is the number of parity check bits. The output of FEC Encoder is denoted by  $\mathbf{c} = [c_1 \ c_2 \ \dots \ c_N] = [u_1 \ u_2 \ \dots \ u_K | p_1 \ p_2 \ \dots \ p_M]$ , where  $N = K + M$  is length of encoder output sequence.

The FEC encoding scheme is shown in Figure x1. The scheme consists of a systematic QC-LDPC encoder and a shortening and puncturing mechanism. The parameters of the FEC encoding scheme are:

- the LDPC parity check matrix is a 13-by-75 quasi-cyclic matrix, with circulant size  $Z = 256$ ; LDPC user bit length before shortening is  $62 \times 256 = 15,872$ , the parity bit length before puncturing is  $13 \times 256 = 3,328$ ; the codeword length before any shortening and puncturing is 19,200;
- the number of transmitted information bits,  $K$  (with maximum user length  $K_{\max} = 15,677$ );
- the number of shortened information bits,  $S$  ( $S_{\min} = 195$ );
- the number of punctured parity check bits,  $P$  ( $P = 512$ );
- the number of parity-check bits after puncturing,  $M$  ( $M = 3,328 - 512 = 2,816$ );
- the number of output bits,  $N$  ( $N = K + M$ , FEC codeword, whose size depends on the burst length pattern to determine shortening length);  $N_{\max} = K_{\max} + M = 18,493$ ;
- the code rate,  $R = K/N$ , defined as the code rate after puncturing and after shortening.

The encoder supports highest code rate  $R_{\max} = \frac{K_{\max}}{N_{\max}} = 0.8477$ . Codes with lower code rates/shorter block length shall be obtained through shortening. The puncturing length and location are fixed for all scenarios.

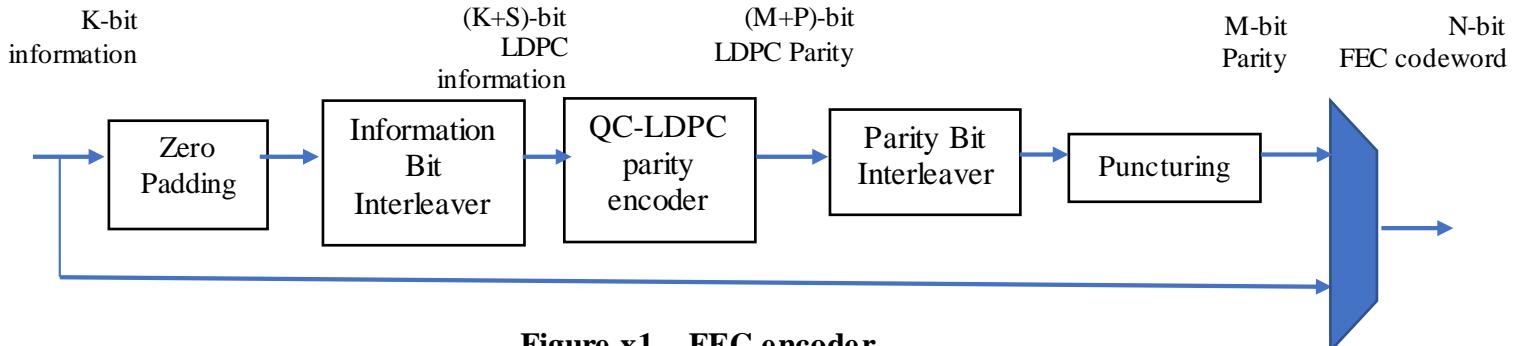


Figure x1 – FEC encoder

## LDPC Encoder

The full LDPC code is defined by a  $(M+P) \times (K+S+M+P) = 3328 \times 19200$  size parity-check matrix  $H$  composed by a  $13 \times 75$  array of  $256 \times 256$  sub-matrices  $A_{i,j}$ :

$$\mathbf{H} = \begin{bmatrix} \mathbf{A}_{1,1} & \cdots & \mathbf{A}_{1,75} \\ \vdots & \ddots & \vdots \\ \mathbf{A}_{13,1} & \cdots & \mathbf{A}_{13,75} \end{bmatrix}$$

The sub-matrices  $\mathbf{A}_{i,j}$  are either a cyclic shifted version of identity matrix or a zero matrix, and have a size of  $256 \times 256$ . The parity-check matrix can be described in its compact form:

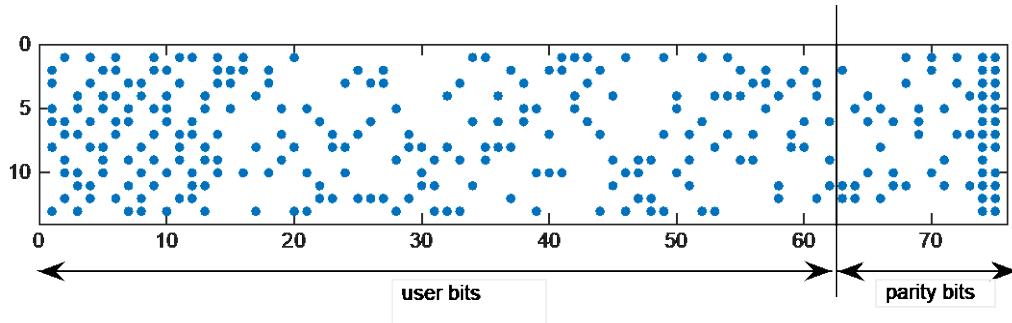
$$\mathbf{H}_c = \begin{bmatrix} a_{1,1} & \cdots & a_{1,75} \\ \vdots & \ddots & \vdots \\ a_{13,1} & \cdots & a_{13,75} \end{bmatrix}$$

where  $a_{i,j} = -1$  for a zero sub-matrix in position  $(i, j)$ , and a positive integer number  $a_{i,j}$  defines the number of right column shifts of the identity matrix.

*Note to Editor (to be removed prior to publication): If the parity matrix font size is too small for publication, suggest following what Clause 55/55A did by having a zip file made downloadable from <http://standards.ieee.org/downloads/802.3/> containing han\_3ca\_1\_0118.txt. Also an option, create larger tables like as was done in Clause 101.*

The compact form of parity-check matrix  $\mathbf{H}_c$  shown below:

Figure x2 is an image of the matrix  $\mathbf{H}_c$  to show non-zero locations, and parity/user bit assignments corresponding to parity check matrix columns. A dot represents a non-zero 256×256 circulant in the  $13 \times 75$  H matrix.



## **Figure x2 – Parity Check Matrix Image**

A fixed amount (512 bits) and locations of the parities are punctured on the full LDPC matrix; a minimum amount (195 bits) and locations of the user bits are shortened on the full LDPC matrix. The effective maximum code rate 0.8477.



**Figure x3 – Codeword Information/Parity Location assignments**

## Encoding Operation

The encoding process shall be as follows:

- 1) A group of  $K$  information bits  $\mathbf{u} = [u_1 \ u_2 \ \dots \ u_K]$  are collected and copied to the output of the encoder to form a block of systematic code bits. They are also the input to the zero-padding block (see Figure x1).
- 2) A total of  $S$  zero bits are appended at the end of  $\mathbf{u}$  to form the full-length information bit vector  $\mathbf{u}^* = [\mathbf{u} | 0, \dots, 0]$ , which is then sent to the information bit interleaver module, which in turn produces the bit-interleaved sequence  $\hat{\mathbf{u}} = \pi_{\text{info}}(\mathbf{u}^*)$ .
- 3) The interleaved LDPC information bits  $\hat{\mathbf{u}}$  is sent to the QC-LDPC parity encoder, and used to compute parity-check bits  $\hat{\mathbf{p}}$  with the parity-check matrix  $\mathbf{H}$ , which is then interleaved to get  $\mathbf{p}^* = \pi_{\text{parity}}(\hat{\mathbf{p}})$ .
- 4)  $M + P$  parity bits  $\mathbf{p}^* = [p_1 \ p_2 \ \dots \ p_M \ | \ p_{M+1} \ \dots \ p_{M+P}]$  are sent to the puncturing block.
- 5) The last  $P$  bits of  $\mathbf{p}^*$  are truncated, and  $M$  parity bits  $\mathbf{p} = [p_1 \ p_2 \ \dots \ p_M]$  are being copied to the output of the encoder to form the parity check bits.
- 6) At the encoder output  $\mathbf{c} = [\mathbf{u} \ | \ \mathbf{p}] = [u_1 \ u_2 \ \dots \ u_K \ | \ p_1 \ p_2 \ \dots \ p_M]$ , such that  $[\hat{\mathbf{u}} \ | \ \hat{\mathbf{p}}] \mathbf{H}^T = \mathbf{0}$ .